

Reservoir Computing

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Contact Information

Research interests:

Learning long-term dependencies with RNNs

Reservoir computing – Randomised NNs

Convolutional neural networks

Modular composition of NNs

Linking cognitive features to attractor's geometries

State space models for sequence learning

Graph Neural Networks

Criticality in complex systems

Dynamical recurrent neural models (bio-inspired)

Do you like these topics? Email me!

email: andrea.ceni@di.unipi.it

My path

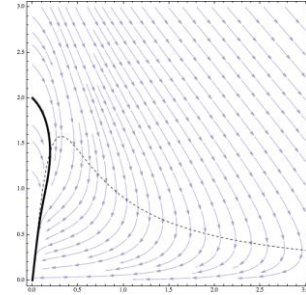
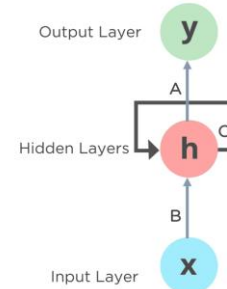
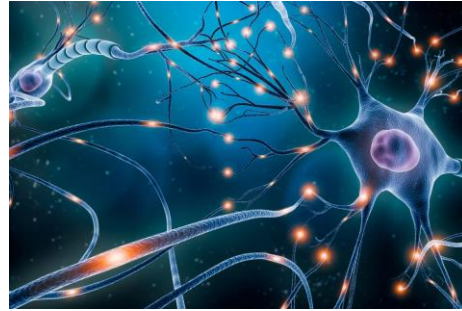
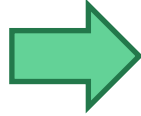


UNIVERSITÀ
DEGLI STUDI
FIRENZE



University
of Exeter

$$\frac{\partial}{\partial a} \ln f_{a, \sigma^2}(\xi_1) = \frac{(\xi_1 - a)}{\sigma^2} f_{a, \sigma^2}(\xi_1) = \frac{1}{\sqrt{2\pi\sigma^2}} \frac{\xi_1 - a}{\sigma^2} e^{-\frac{(\xi_1 - a)^2}{2\sigma^2}}$$
$$\int_{\mathbb{R}_+} \mathcal{T}(x) \cdot \frac{\partial}{\partial \theta} f(x, \theta) dx = M \left(\mathcal{T}(\xi) \cdot \frac{\partial}{\partial \theta} \ln l(\xi, \theta) \right)$$
$$\int_{\mathbb{R}_+} \mathcal{T}(x) \cdot \left(\frac{\partial}{\partial \theta} \ln l(x, \theta) \right) \cdot f(x, \theta) dx = \int_{\mathbb{R}_+} \mathcal{T}(x) \cdot \left(\frac{\partial}{\partial \theta} f(x, \theta) \right) dx$$
$$\frac{\partial}{\partial \theta} \int_{\mathbb{R}_+} \mathcal{T}(x) f(x, \theta) dx = \int_{\mathbb{R}_+} \mathcal{T}(x) \frac{\partial}{\partial \theta} f(x, \theta) dx$$

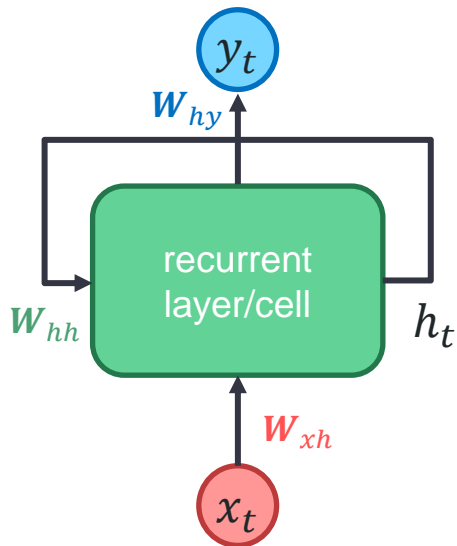


Reservoir Computing

=

Extremely efficient way of
designing and training RNNs

Recurrent Neural Networks



- State update:

$$h_t = \tanh(x_t W_{xh} + h_{t-1} W_{hh})$$

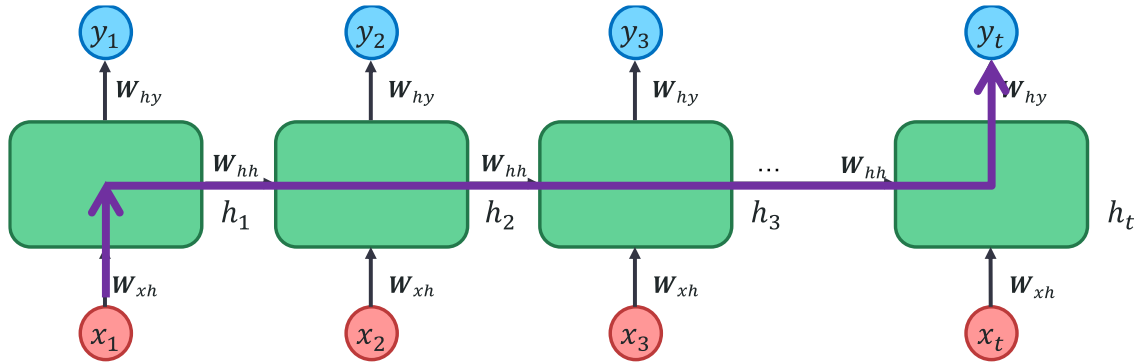
input
state
previous state
input weight matrix
recurrent weight matrix

- Output function:

$$y_t = h_t W_{hy}$$

output
state
output weight matrix

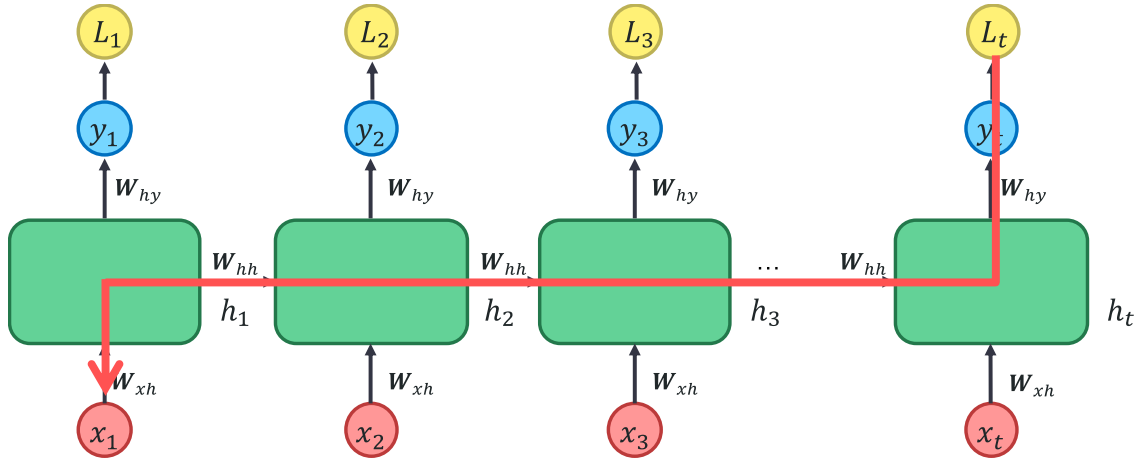
Forward Computation



Fading/Exploding memory:

- the influence of inputs far in the past vanishes/explodes in the current state
- many (non-linear) transformations

Backpropagation Through Time (BPTT)



Gradient Propagation

- gradient might vanish/explode through many non-linear transformations
- difficult to train on long-term dependencies

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Ceni, A. (2022). Random orthogonal additive filters: a solution to the vanishing/exploding gradient of deep neural networks. *arXiv preprint arXiv:2210.01245*.

Approaches

- **Gated architectures**

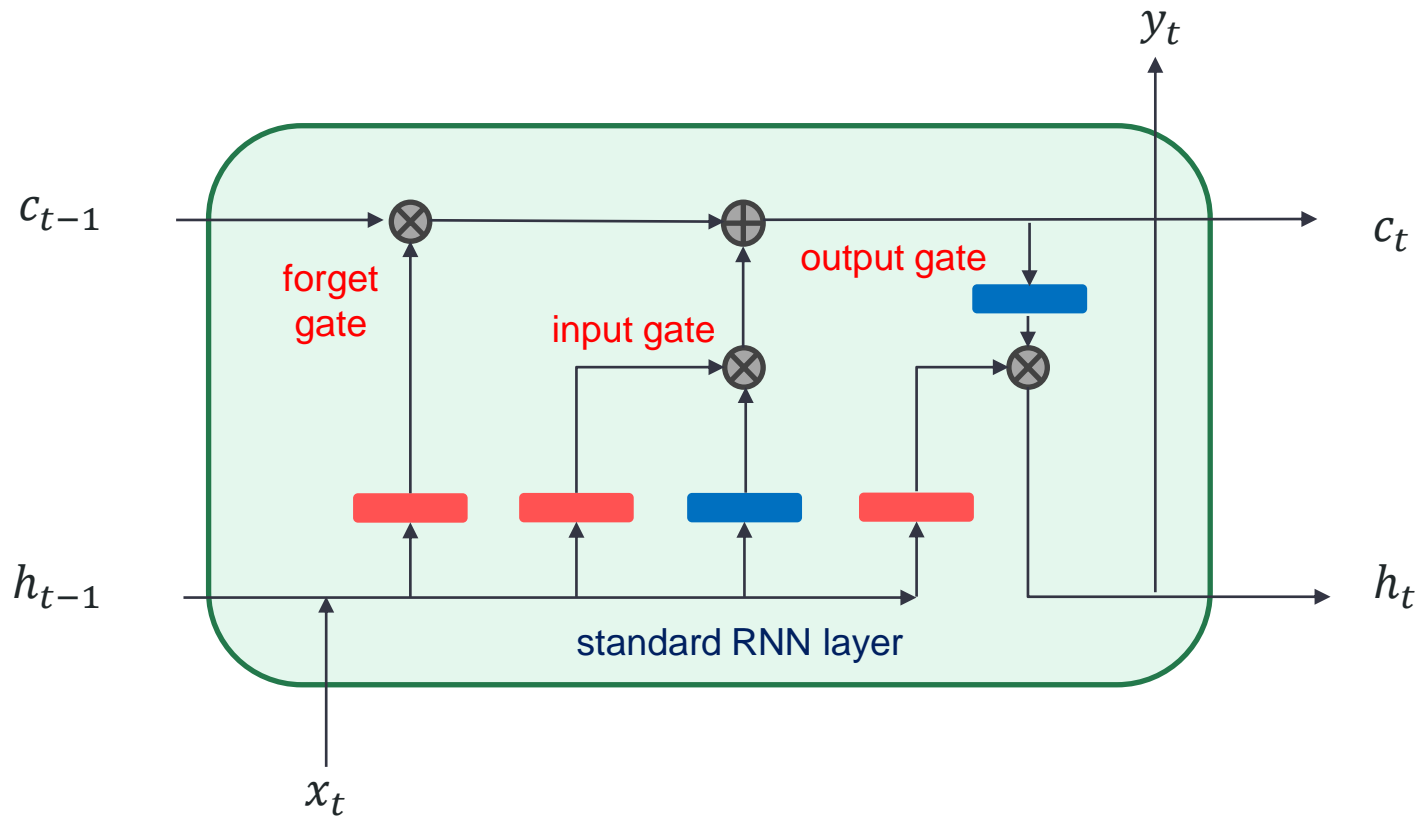
- create a pathway for uninterrupted gradient propagation
- LSTM, GRU
- training is slow



- **Smart initialization**

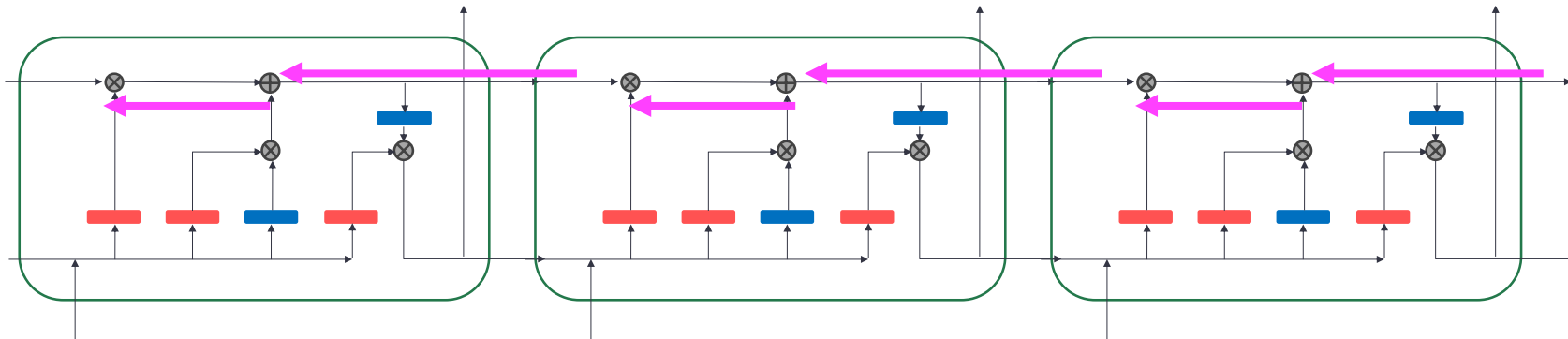
- Reservoir Computing
- training is limited

LSTM cell



Long-term dependencies

gradient computation flow without interruptions



LSTM equations

vanilla RNN

- $g_t = \tanh(h_{t-1}W_{hg} + x_t W_{xg} + b_g)$

- $f_t = \sigma(h_{t-1}\underline{W_{hf}} + x_t \underline{W_{xf}} + \underline{b_f})$

- $i_t = \sigma(h_{t-1}\underline{W_{hi}} + x_t \underline{W_{xi}} + \underline{b_i})$

extra computation

- $c_t = f_t \otimes c_{t-1} + i_t \otimes g_t$

- $o_t = \sigma(h_{t-1}\underline{W_{ho}} + x_t \underline{W_{xo}} + \underline{b_o})$

- $h_t = o_t \otimes \tanh(c_t)$

extra parameters



training is slow
(computationally intensive)

The Philosophy

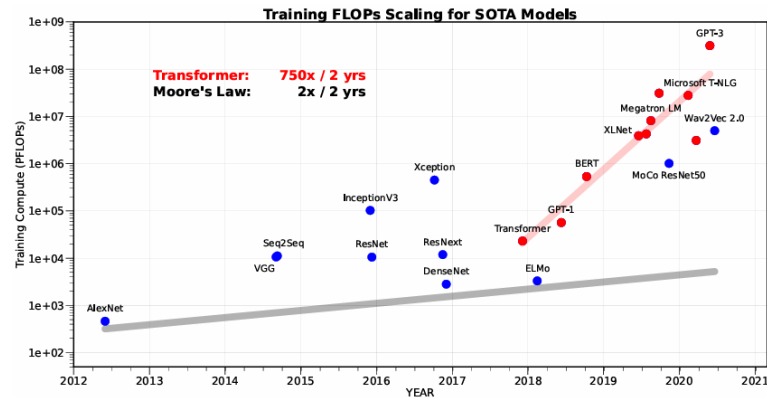
“Randomization is
computationally cheaper than
optimization”

Rahimi, A. and Recht, B., 2008. Weighted sums of random kitchen sinks: Replacing minimization with randomization in learning. *Advances in neural information processing systems*, 21, pp.1313-1320.

Rahimi, A. and Recht, B., 2007. Random features for large-scale kernel machines. *Advances in neural information processing systems*, 20, pp. 1177-1184.

Energy consumption matters!

AlexNet to AlphaGo Zero: A 300,000x Increase in Compute (Log Scale)



Gholami, Amir, et al. "Ai and memory wall." *IEEE Micro* (2024).

- 2012-2017: 300000x
- 3.4-month doubling time

Dario Amodei and Danny Hernandez. AI and compute, 2018. Blog post.

<https://openai.com/blog/ai-and-compute/>

Green AI

Roy Schwartz*[◇] Jesse Dodge*^{◇♣} Noah A. Smith^{◇♡} Oren Etzioni[◇]

[◇] Allen Institute for AI, Seattle, Washington, USA

[♣] Carnegie Mellon University, Pittsburgh, Pennsylvania, USA

[♡] University of Washington, Seattle, Washington, USA

July 2019

Abstract

The computations required for deep learning research have been doubling every few months, resulting in an estimated 300,000x increase from 2012 to 2018 [2]. These computations have a surprisingly large carbon footprint [40]. Ironically, deep learning was inspired by the human brain, which is remarkably energy efficient. Moreover, the financial cost of the computations can make it difficult for academics, students, and researchers, in particular those from emerging economies, to engage in deep learning research.

This position paper advocates a practical solution by making **efficiency** an evaluation criterion for research alongside accuracy and related measures. In addition, we propose reporting the financial cost or “price tag” of developing, training, and running models to provide baselines for the investigation of increasingly efficient methods. Our goal is to make AI both greener and more inclusive—enabling any inspired undergraduate with a laptop to write high-quality research papers. **Green AI** is an emerging focus at the Allen Institute for AI.

Schwartz, Roy, et al.
"Green ai." *arXiv preprint*
arXiv:1907.10597 (2019).

Quantifying the carbon emissions of ML

ML CO2 Impact Compute Publish Learn Act About

Machine Learning Emissions Calculator

Choose your hardware, runtime and cloud provider to estimate the carbon impact of your research.

This calculator will give you 2 numbers: the **raw** carbon emissions produced and the approximate **offset** carbon emissions. The latter number depends on the grid used by the cloud provider and we are open to update our estimates if anything looks inaccurate or outdated.

Also, keep in mind that the estimate provided below **does not** take datacenter PUE (Power Usage Effectiveness) into account. To do so, you need to find your datacenter's PUE (by asking your computer provider or consulting their documentation) and multiply the quantity of carbon emitted provided below by that number.

Missing a Hardware or a region? Open an issue or a PR on [Github](#)

Hardware type: A100 PCIe 40/80G ▾

Hours Used: 336

Provider: Google Cloud Plat ▾

Region of Compute: europe-west1 ▾

COMPUTE

<https://mlco2.github.io/impact/>

22.68 kg of CO₂eq. is equivalent to:

11.3

Kgs of coal burned ^[2]

Lacoste, Alexandre, et al.
"Quantifying the carbon emissions of machine learning." *arXiv preprint arXiv:1910.09700* (2019).

Energy consumption matters!

Artificial intelligence / Machine learning

Training a single AI model can emit as much carbon as five cars in their lifetimes

Deep learning has a terrible carbon footprint.

by **Karen Hao**

June 6, 2019

The artificial-intelligence industry is often compared to the oil industry: once mined and refined, data, like oil, can be a highly lucrative commodity. Now it seems the metaphor may extend even further. Like its fossil-fuel counterpart, the process of deep learning has an outsize environmental impact.

ImageNet Training in 24 Minutes

Yang You, Zhao Zhang, James Demmel, Kurt Keutzer, Cho-Jui Hsieh

(Submitted on 14 Sep 2017)

Finishing 90-epoch ImageNet-1k training with ResNet-50 on a NVIDIA M40 GPU takes 14 days. This training requires 10^{18} single precision operations in total. On the other hand, the world's current fastest supercomputer can finish $2 * 10^{17}$ single precision operations per second (Dongarra et al 2017). If we can make full use of the supercomputer for DNN training, we should be able to finish the 90-epoch ResNet-50 training in five seconds. However, the current bottleneck for fast DNN training is in the algorithm level. Specifically, the current batch size (e.g. 512) is too small to make efficient use of many processors

For large-scale DNN training, we focus on using large-batch data-parallelism synchronous SGD without losing accuracy in the fixed epochs. The LARS algorithm (You, Gitman, Ginsburg, 2017) enables us to scale the batch size to extremely large case (e.g. 32K). We finish the 100-epoch ImageNet training with AlexNet in 24 minutes, which is the world record. Same as Facebook's result (Goyal et al 2017), we finish the 90-epoch ImageNet training with ResNet-50 in one hour

However, our hardware budget is only 1.2 million USD, which is 3.4 times lower than Facebook's 4.1 million USD.

Yet another accelerated sgd: Resnet-50 training on imagenet in 74.7 seconds

[M Yamazaki, A Kasagi, A Tabuchi, T Honda...](#) - arXiv preprint arXiv ..., 2019 - arxiv.org

... on ImageNet using 81,920 mini-batch size in 74.7 seconds. ... -50 training on ImageNet in 74.7 seconds with 75.08% ... 2, the dotted line denotes the ideal throughput of images-per-second, ...

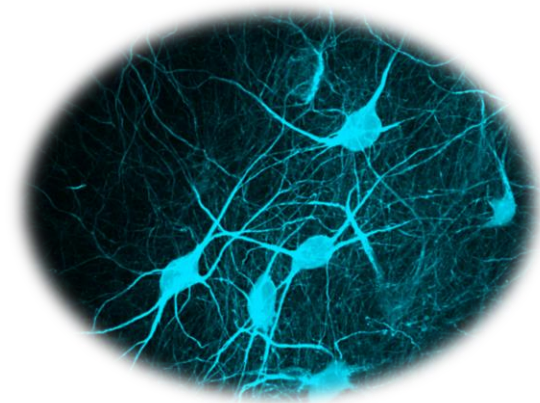
vs the Brain...

...Neuromorphic Computing



≈30 PFlops

10 MW vs 20 W



memory and computing are co-located

10^{11} neurons, 10^{15} synapses

10000 synapses/neuron

Deep Learning

Deep Learning models achieved tremendous success over the years. This comes at very high cost in terms of

- Time
- Parameters

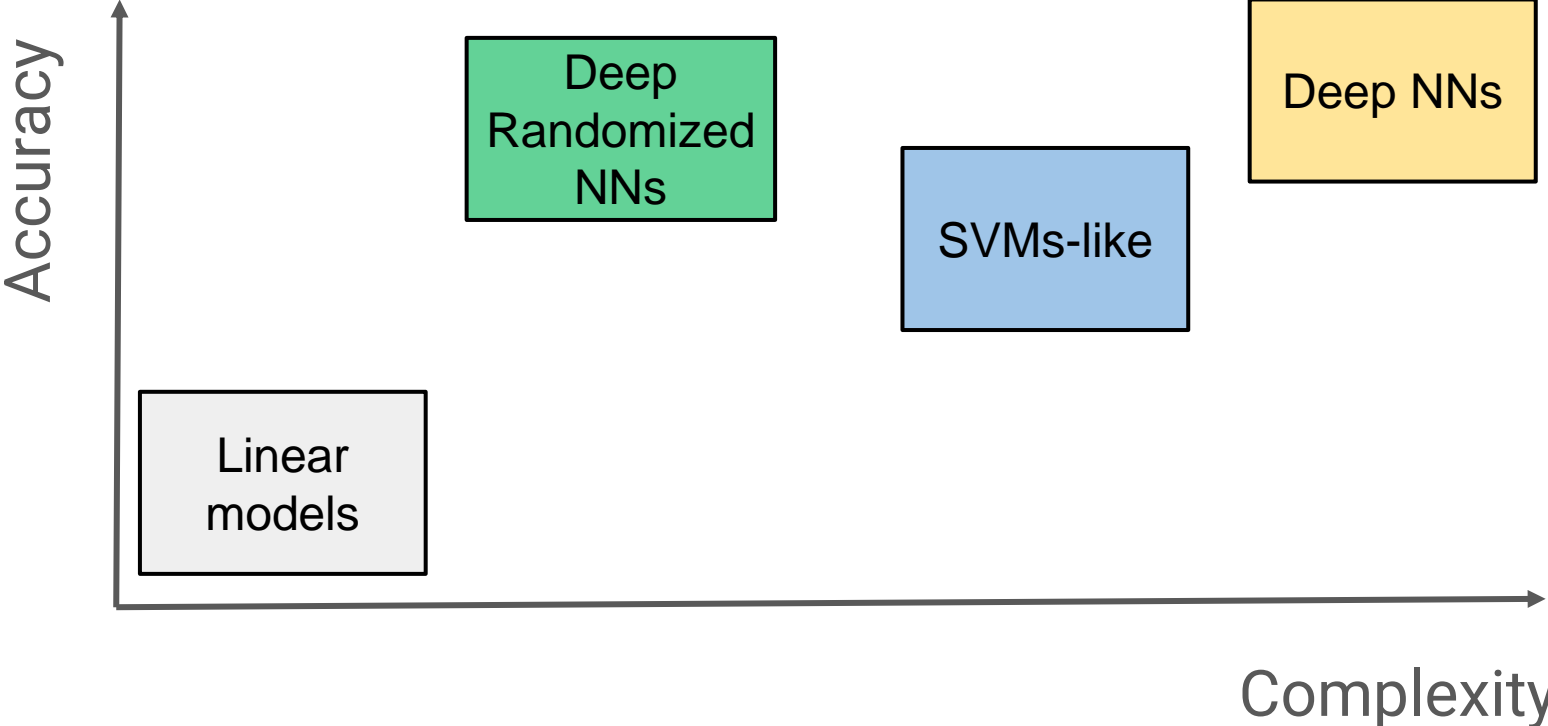
Do we really need this all the time?

Deep Neural Networks

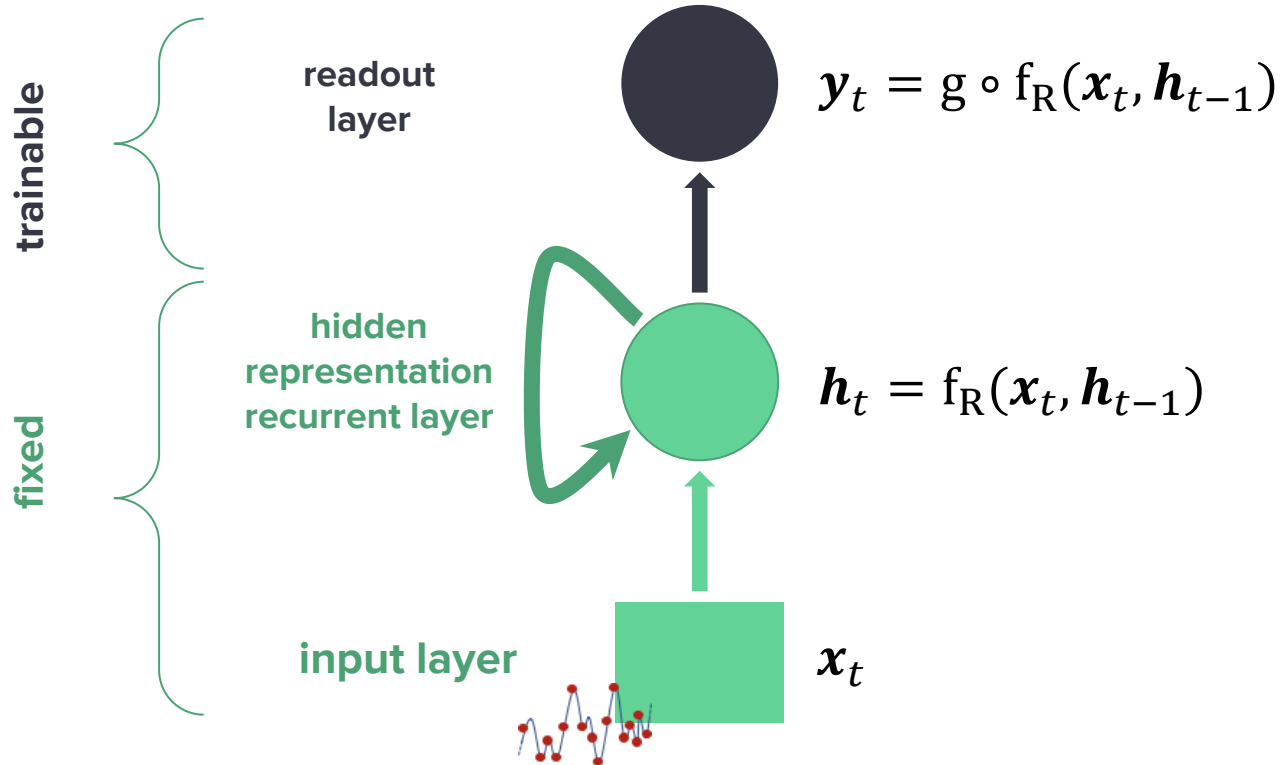
Powerful representations by applying multiple non-linear levels of transformation

Deep Learning = Architectural Biases + Learning Algorithms

Complexity / Accuracy Tradeoff



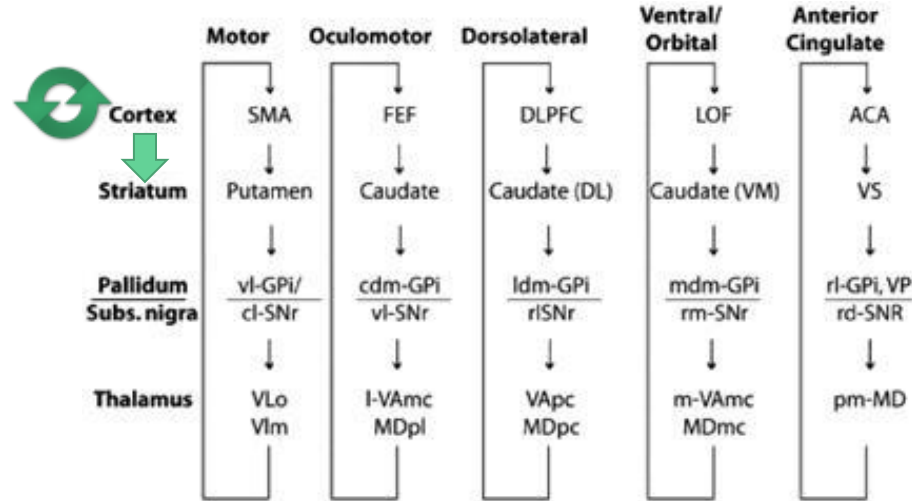
Randomized Recurrent Neural Networks



Randomization = Efficiency

- Training algorithms are cheaper and simpler
- Model transfer: don't need to transmit all the weights
- Amenable to neuromorphic implementations

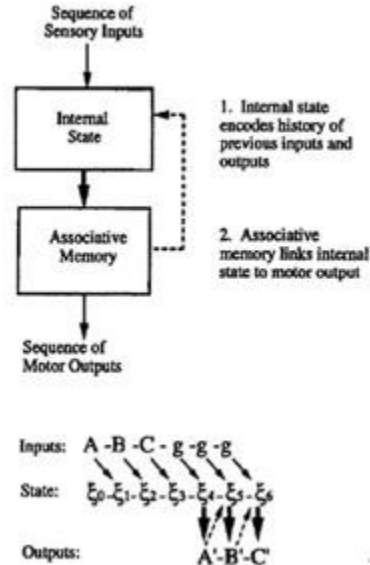
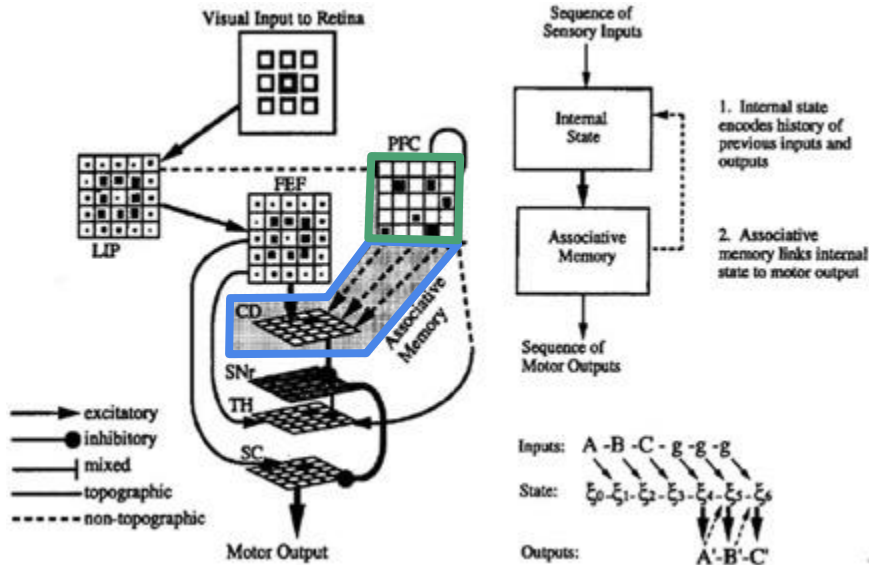
Historical note: the cortico-striatal model



- Structured projections from cortex to striatum is a major architectural property of primate brains
- Recurrent cortico-cortical connections
- Dopamine-regulated plasticity in cortico-striatal connections

Dominey, P.F., 2013. Recurrent temporal networks and language acquisition—from corticostriatal neurophysiology to reservoir computing. *Frontiers in psychology*, 4, p.500.

Historical note: the cortico-striatal model

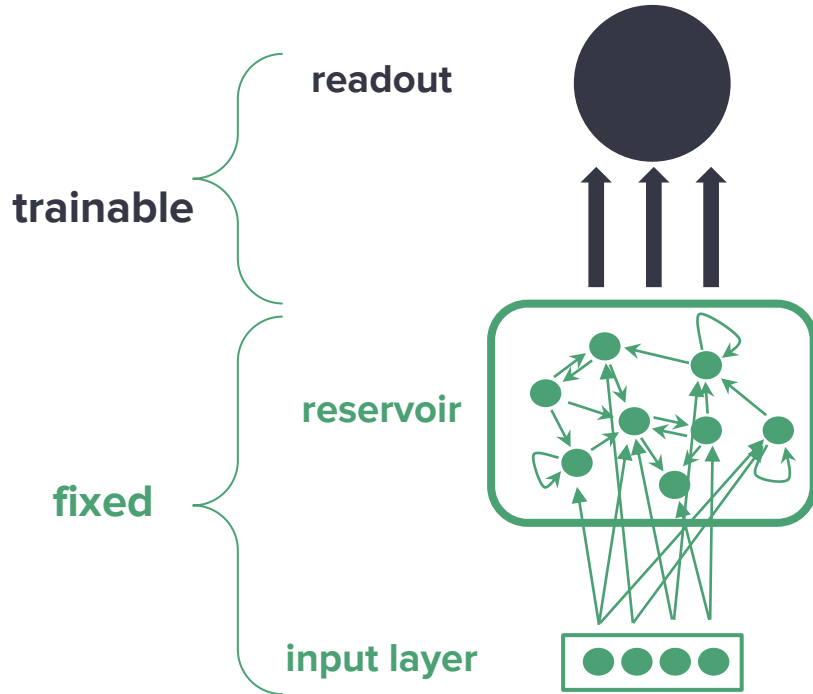


- Fixed recurrent connections in the PFC
- Modifiable connections between PFC and neurons in the striatum (CD)

Dominey, P.F., 2013. Recurrent temporal networks and language acquisition—from corticostriatal neurophysiology to reservoir computing. *Frontiers in psychology*, 4, p.500.

Reservoir Computing

Reservoir Computing: focus on the dynamical system



$$\mathbf{h}_t = \tanh(\mathbf{x}_t \mathbf{W}_{xh} + \mathbf{h}_{t-1} \mathbf{W}_{hh})$$

Randomly initialized under stability conditions on the dynamical system

Stable dynamics - Echo State Property

Verstraeten, David, et al. *Neural networks* 20.3 (2007).
Lukoševičius, Mantas, and Herbert Jaeger. *Computer Science Review* 3.3 (2009).

Echo State Network

REPORTS

Harnessing Nonlinearity: Predicting Chaotic Systems and Saving Energy in Wireless Communication

Herbert Jaeger* and Harald Haas

We present a method for learning nonlinear systems, echo state networks (ESNs). ESNs employ artificial recurrent neural networks in a way that has recently been proposed independently as a learning mechanism in biological brains. The learning method is computationally efficient and easy to use. On a benchmark task of predicting a chaotic time series, accuracy is improved by a factor of 2400 over previous techniques. The potential for engineering applications is illustrated by equalizing a communication channel, where the signal error rate is improved by two orders of magnitude.

Liquid State Machine

ARTICLE  Communicated by Rodney Douglas

Real-Time Computing Without Stable States: A New Framework for Neural Computation Based on Perturbations

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Fractal Prediction Machine

Predicting the Future of Discrete Sequences from Fractal Representations of the Past

PETER TIÑO

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GEORG DORFFNER

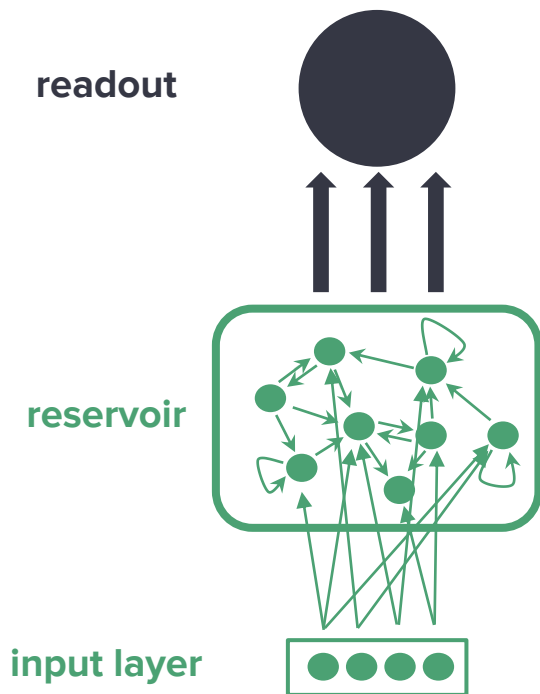
georg@ai.univie.ac.at

Austrian Research Institute for Artificial Intelligence, Schottengasse 3, A-1010 Vienna, Austria; Department of Medical Cybernetics and Artificial Intelligence, University of Vienna, Freyung 6/2, A-1010 Vienna, Austria

Editor: Michael Jordan

Abstract. We propose a novel approach for building finite memory predictive models similar in spirit to variable memory length Markov models (VLMs). The models are constructed by first transforming the n -block structure of the training sequence into a geometric structure of points in a unit hypercube, such that the longer is the common suffix shared by any two n -blocks, the closer lie their point representations. Such a transformation embodies a Markov assumption— n -blocks with long common suffixes are likely to produce similar continuations. Prediction contexts are found by detecting clusters in the geometric n -block representation of the training sequence via vector quantization. We compare our model with both the classical (fixed order) and variable memory length Markov models on five data sets with different memory and stochastic components. Fixed order Markov models (MMs) fail on three large data sets on which the advantage of allowing variable memory length can be exploited. On these data sets, our predictive models have a superior, or comparable performance to that of VLMs, yet, their construction is fully automatic, which, is shown to be problematic in the case of VLMs. On one data set, VLMs are outperformed by the classical MMs. On this set, our models perform significantly better than MMs. On the remaining data set, classical MMs outperform the variable context length strategies.

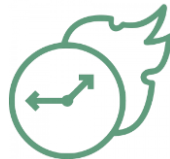
Echo State Networks (ESNs)



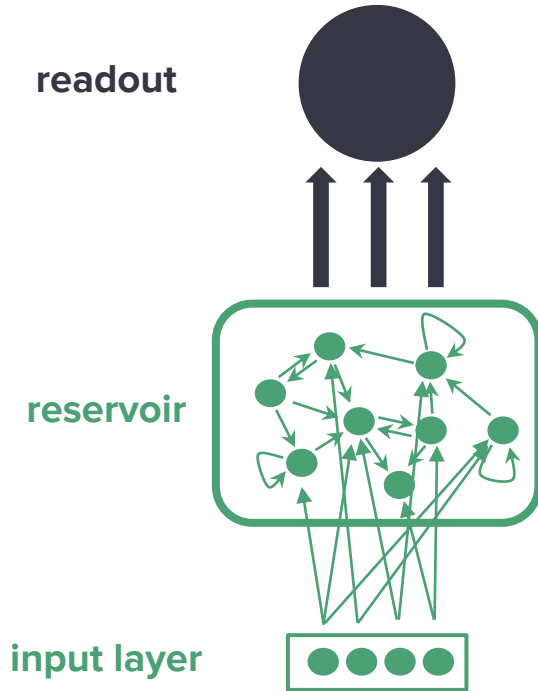
Reservoir

$$h_t = \tanh(x_t W_{xh} + h_{t-1} W_{hh})$$

- large layer of recurrent units
- sparsely connected
- randomly initialized under the ESP
- untrained



Echo State Networks (ESNs)



Readout

$$y_t = h_t W_{hy}$$

- **linear** combination of the reservoir state variables
- can be trained in closed form

$$W_{hy} = (H^T H)^{-1} H^T D$$

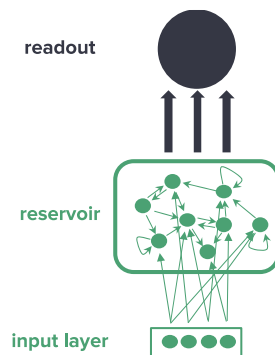
ESNs in a nutshell



- **Architecture of the Echo State Network:**
 - Reservoir: untrained non-linear recurrent hidden layer
 - Readout: (linear) output layer
- **Setup of the Neural Network:**
 - Initialize W_{xh} and W_{hh} randomly
 - Scale W_{hh} to meet the contractive/stability property
- **Training of the Neural Network**
 - Drive the network with the input signal
 - Discard an initial transient
 - Train the readout

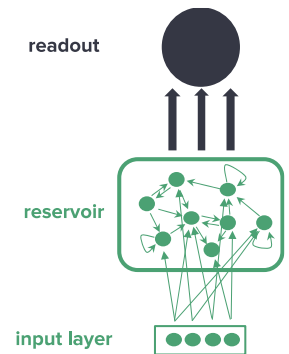
Reservoir

- **Non-linearly embed the input into a higher dimensional feature space** where the original problem is more likely to be solved linearly (Cover's Th.)
- **Randomized basis expansion** computed by a pool of randomized filters
- Provides a “rich” set of input-driven dynamics



Readout

- Use the features in the reservoir state space for the output computation
- Typically implemented by using **linear models**
- Learning involves **convex optimization**



Reservoir: State Transition Function

Reservoir = discrete-time input-driven dyn. system

- Dynamics are driven by the state transition function

$$F: \mathbb{R}^{N_X} \times \mathbb{R}^{N_H} \rightarrow \mathbb{R}^{N_H}$$

$$\begin{aligned} \mathbf{h}_t &= F(\mathbf{x}_t, \mathbf{h}_{t-1}) \\ &= \tanh(\mathbf{x}_t \mathbf{W}_{xh} + \mathbf{h}_{t-1} \mathbf{W}_{hh}) \end{aligned}$$

Reservoir: State Transition Function

Iterated version of state transition function

- given an input sequence $s = [x_1, x_2, \dots, x_t]$
- return the final state h_t

$$\hat{F}: (\mathbb{R}^{N_X})^* \times \mathbb{R}^{N_H} \rightarrow \mathbb{R}^{N_H}$$

The diagram illustrates the function \hat{F} which takes an input sequence s and an initial state h_0 as input and returns a final state h_t . Green arrows point from the labels 'input sequence s ', 'initial state h_0 ', and 'final state h_t ' to their respective parts in the function signature.

Reservoir: State Transition Function

Iterated version of state transition function

$$\hat{F}(s, \mathbf{h}_0) = \begin{cases} \mathbf{h}_0 & \text{if } s = [] \\ F(\mathbf{x}_t, \underline{\hat{F}([\mathbf{x}_1, \dots, \mathbf{x}_{t-1}], \mathbf{h}_0)}) & \text{if } s = [\mathbf{x}_1, \dots, \mathbf{x}_t] \end{cases}$$

iterated application:
the state after seeing all but 1 input

Echo State Property (ESP)

Yildiz, Izzet B., Herbert Jaeger, and Stefan J. Kiebel. "Re-visiting the echo state property." *Neural networks* 35 (2012): 1-9.

A valid ESN should satisfy the “Echo State Property”

- (DEF) An ESN satisfies the ESP whenever:

$$\forall \mathbf{s} \in (\mathbb{R}^{N_X})^N, \forall \mathbf{h}_0, \mathbf{z}_0 \in \mathbb{R}^{N_H}:$$

input sequence of length N couple of initial states

$$\|\hat{F}(\mathbf{s}, \mathbf{h}_0) - \hat{F}(\mathbf{s}, \mathbf{z}_0)\| \rightarrow 0, \quad \text{as } N \rightarrow \infty$$

the distance between the final states goes to 0

Echo State Property

- The state of the network asymptotically depends only on the driving input signal
- Dependencies on the initial conditions are progressively lost
- Fading memory

Conditions for the ESP

- **Sufficient Condition**, involving the control of the maximum singular value of W_{hh}
- **Necessary Condition**, involving the control of the maximum eigenvalue in modulus of W_{hh}
- Active area of intense mathematical research: link it to the input



Sufficient Condition for the ESP

- **Theorem.** If the maximum singular value of \mathbf{W}_{hh} is < 1 then (under mild assumptions) the ESN satisfies the ESP for any possible input.

Sufficient condition for the ESP

- contractive dynamics for every input

$$\sigma_{max}(\mathbf{W}_{hh}) = \|\mathbf{W}_{hh}\|_2 < 1$$

Necessary Condition for the ESP

- **Theorem.** If the spectral radius of \mathbf{W}_{hh} is not smaller than 1 then (under mild assumptions) the ESN does not satisfy the ESP.

Necessary condition for the ESP

- globally asymptotically stable dynamics around the 0 state

$$\rho(\mathbf{W}_{hh}) = \max(\text{abs}(\text{eig}(\mathbf{W}_{hh}))) < 1$$

Relation between the ESP conditions

- Known linear algebra fact: $\rho(\mathbf{W}_{hh}) \leq \|\mathbf{W}_{hh}\|_n$
- Applying the **sufficient condition** is OK in theory, but often impractical: it is **too strong!**
- **Often, the necessary condition is used** as an easy way for initialization of the reservoir

Reservoir Initialization

Initialization of W_{hh} :

- 1) Generate a random matrix W
e.g. from a uniform distribution on $[-1,1]$
- 2) Scale by the desired spectral radius

$$W_{hh} \leftarrow \rho_{desired} \frac{W}{\rho(W)}$$

- Note that now $\rho(W_{hh}) = \rho_{desired}$ (choose a value < 1)
- The spectral radius is a key hyper-parameter of the reservoir

Reservoir Initialization

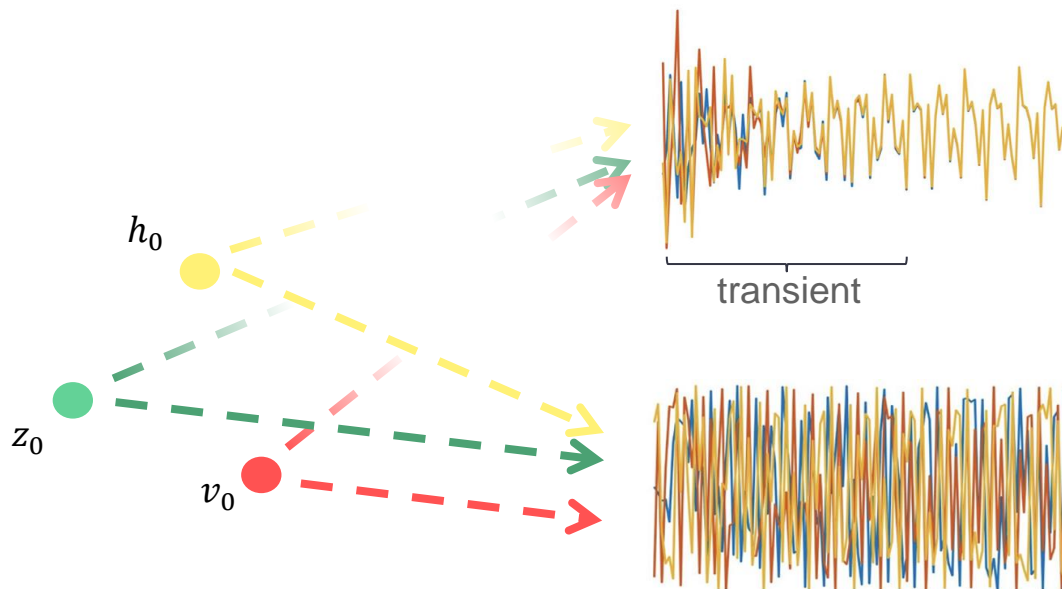
Initialization of W_{xh} :

- 1) Generate a random matrix W_{xh} , whose elements are drawn e.g. from a uniform distribution on $[-1,1]$
 - 2) Scale by an input scaling parameter ω_{in}
 - by range: $W_{xh} \leftarrow \omega_{in} W_{xh}$ (now weights are in $[-\omega_{in}, \omega_{in}]$)
 - by norm: $W_{xh} \leftarrow \omega_{in} \frac{W_{xh}}{\|W_{xh}\|_2}$ (now the 2-norm of W_{xh} equals ω_{in})
- The input scaling is a key hyper-parameter of the reservoir

Dynamical Transient

- If the system is globally asymptotically stable, then all possible (input-driven) trajectories will synchronize *after a transient*
- **Washout:** initial part of the time-series in which the state could be still affected by initialization condition (i.e. here the ESP could still not hold)
 - the washout states of the reservoir should be discarded

Stability in Practice



Stable dynamics

- orbits synchronize after a transient

Unstable dynamics

- orbits are sensitive to initial conditions

ESN Training

Given a training set $\{(\mathbf{x}_t, \mathbf{d}_t)\}_{t=1}^N$

1. Run the reservoir on the input sequence & collect the states

$$\mathbf{H} = [\mathbf{h}_1, \dots, \mathbf{h}_N]$$

2. Washout the initial transient. $\mathbf{H} \leftarrow \mathbf{H}(N_w:N, :)$

3. Collect the target data similarly into a matrix

$$\mathbf{D} = [\mathbf{d}_{N_w}, \dots, \mathbf{d}_N]$$

4. Solve the linear regression problem for the readout

$$\min_{\mathbf{W}_{hy}} \|\mathbf{H}\mathbf{W}_{hy} - \mathbf{D}\|_2^2$$

Readout Training

- Typically training performed off-line in closed-form
 - pseudo-inverse $W_{hy} = (H^T H)^{-1} H^T D$
 - ridge-regression $W_{hy} = (H^T H + \lambda I)^{-1} H^T D$
 - Tikhonov regularizer
- Online learning by Least Mean Squares has problems
 - high eigenvalue spread of H
 - alternatives: Recursive Least Squares
 - ... use any other modern optimizer for training the readout layer, use deep readouts

Hyper-parameters tuning by model selection

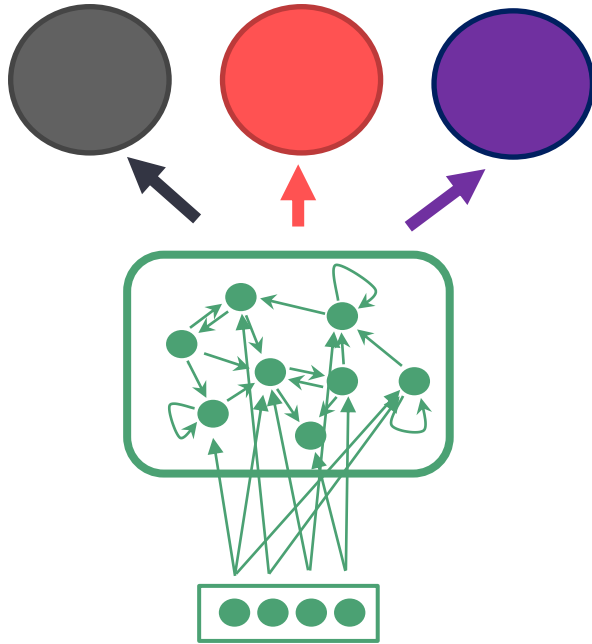
Like for any other ML/NN model, hyp-params tuning is important in applications

- reservoir dimension N_H
- spectral radius ρ
- input scaling ω_{in}
- readout regularization λ
- ...

Practical tips

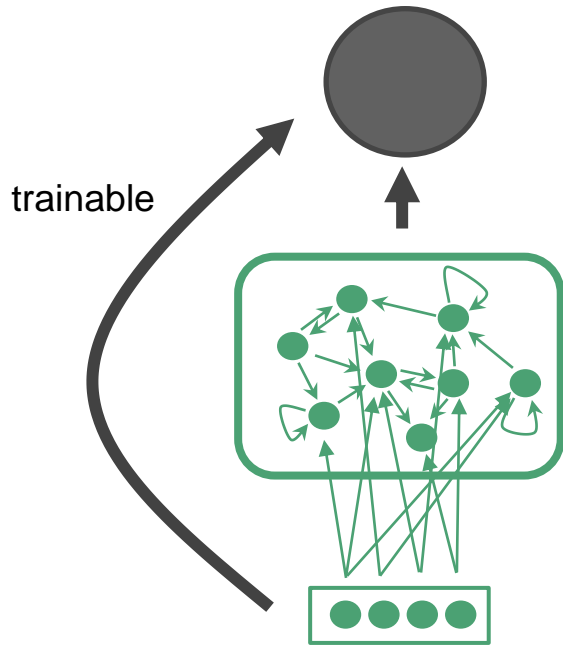
- Using sparse reservoir matrices to boost computing times
- Using $\rho < 1$ gives the ESP in practice in most situations
 - in fine-tuning explore also values >1 (e.g., $\rho \in (0.1, 1.5)$)
- Use larger values of ρ when more memory is needed
- In case of time-series regression:
 - For long sequences discard an initial transient
- In case of time-series classification:
 - Use the last state as representative for the whole input sequence

Architectural variants: Multiple readouts



- The reservoir is operating in unsupervised mode
- The same reservoir can serve to tackle multiple learning problems

Architectural variants: Input-Readout connections



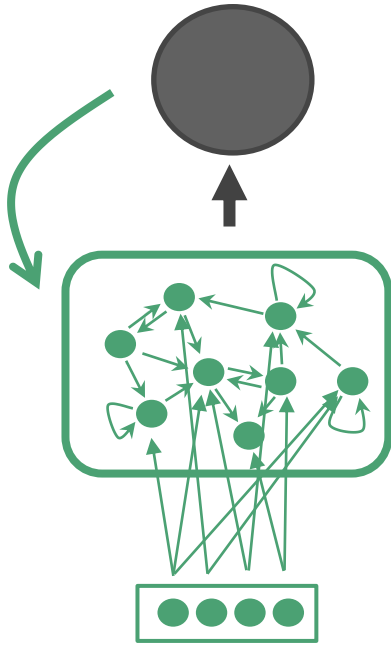
Direct input-readout connections

$$\mathbf{h}_t = \tanh(\mathbf{x}_t \mathbf{W}_{xh} + \mathbf{h}_{t-1} \mathbf{W}_{hh})$$

$$\mathbf{y}_t = [\mathbf{h}_t; \mathbf{x}_t] \mathbf{W}_{hy}$$

useful, e.g., when instantaneous (i.e., non-temporal) I/O transformations can be useful

Architectural Variants: Output feedback



Feedback connections from the readout

$$y_t = \mathbf{h}_t \mathbf{W}_{hy}$$

$$\mathbf{h}_t = \tanh(\mathbf{x}_t \mathbf{W}_{xh} + \mathbf{h}_{t-1} \mathbf{W}_{hh} + y_{t-1} \mathbf{W}_{yh})$$

Might impact on the stability of the reservoir dynamics.

Note: in this case the reservoir dynamics are adapted...

$$\mathbf{h}_t = \tanh(\mathbf{x}_t \mathbf{W}_{xh} + \mathbf{h}_{t-1} (\mathbf{W}_{hh} + \mathbf{W}_{hy} \mathbf{W}_{yh}))$$

Leaky Integrator ESN (LI-ESN)

Use leaky integrators reservoir neurons:

$$\mathbf{h}_t = (1 - \underline{\alpha})\mathbf{h}_{t-1} + \underline{\alpha} \tanh(\mathbf{x}_t \mathbf{W}_{xh} + \mathbf{h}_{t-1} \mathbf{W}_{hh})$$

leaking rate hyper-parameter
 $\alpha \in (0,1]$

A few examples of RC applications

Reservoir Computing in practice

A Practical Guide to Applying Echo State Networks

Mantas Lukoševičius

Jacobs University Bremen, Campus Ring 1,
28759 Bremen, Germany
`m.lukosevicius@jacobs-university.de`

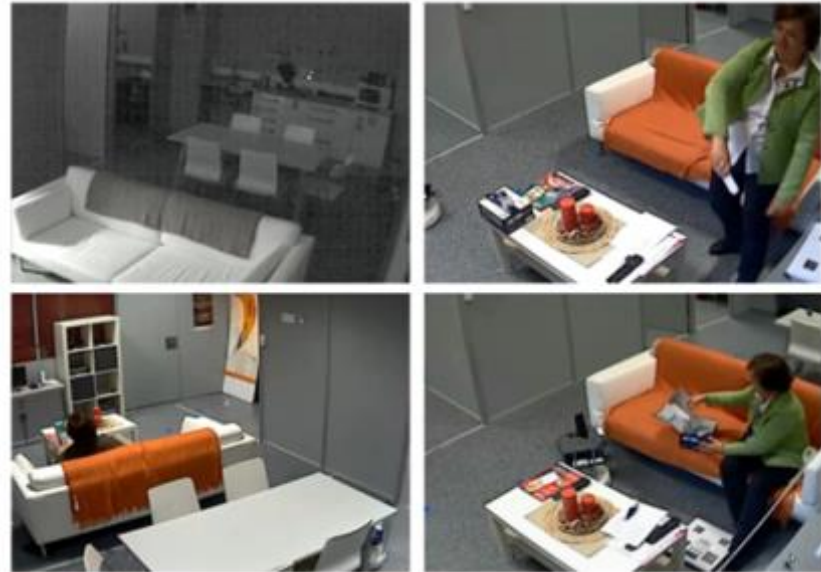
Lukoševičius, M., 2012. A practical guide to applying echo state networks. In Neural networks: Tricks of the trade (pp. 659-686). Springer, Berlin, Heidelberg.

Abstract. Reservoir computing has emerged in the last decade as an alternative to gradient descent methods for training recurrent neural networks. Echo State Network (ESN) is one of the key reservoir computing “flavors”. While being practical, conceptually simple, and easy to implement, ESNs require some experience and insight to achieve the hailed good performance in many tasks. Here we present practical techniques and recommendations for successfully applying ESNs, as well as some more advanced application-specific modifications.

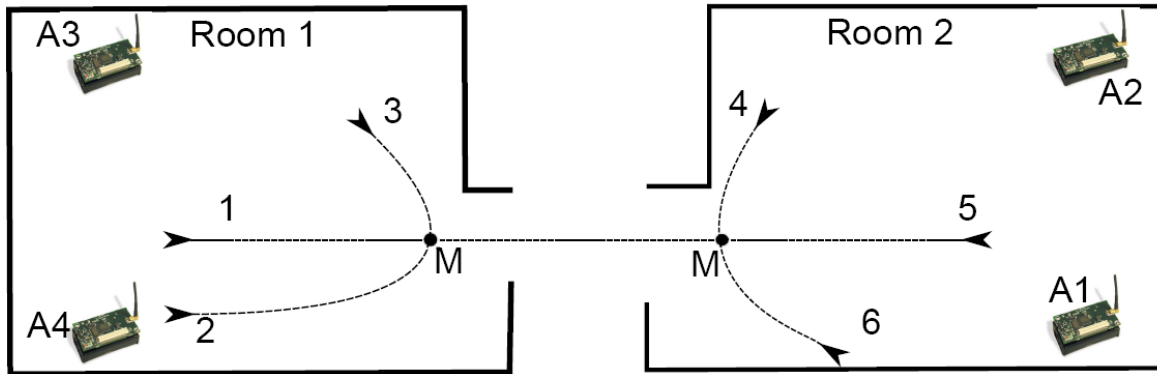
Distributed Intelligence Applications



Dragone, Mauro, et al. "A cognitive robotic ecology approach to self-configuring and evolving AAL systems." *Engineering Applications of Artificial Intelligence* 45 (2015): 269-280.



Human Activity Monitoring



Forecasting human indoor mobility

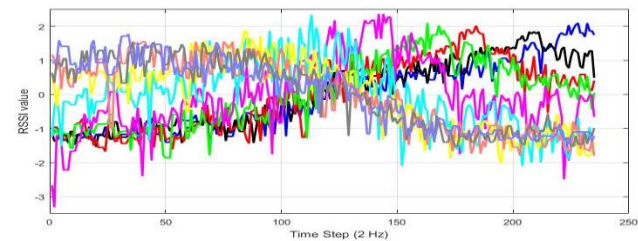
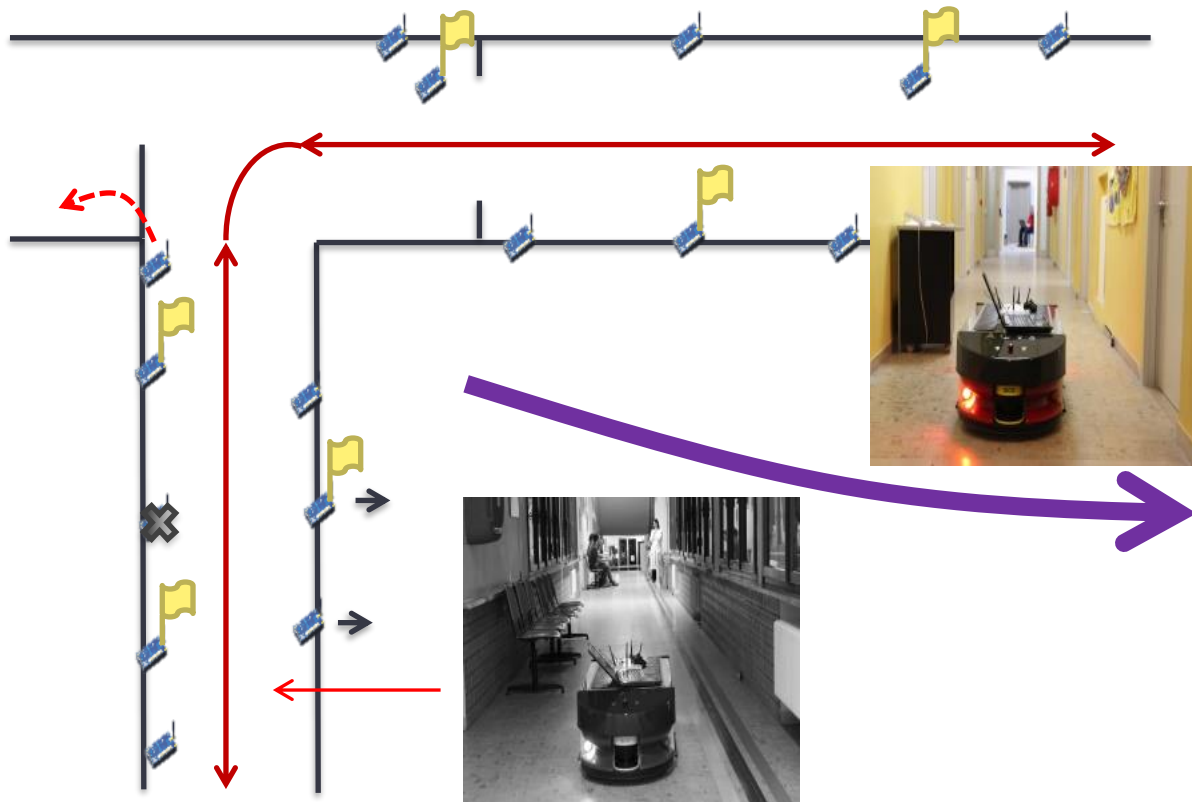


Dataset is available online on the UCI repository

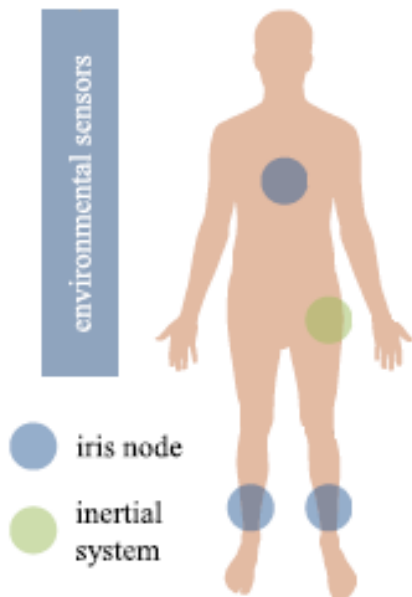
<https://archive.ics.uci.edu/ml/datasets/Indoor+User+Movement+Prediction+from+RSS+data>



Robot localization in critical environments



Human Activity Recognition



- Classification of human daily activities from RSS data generated by sensors worn by the user



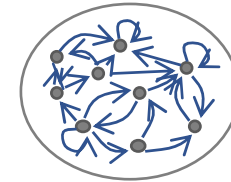
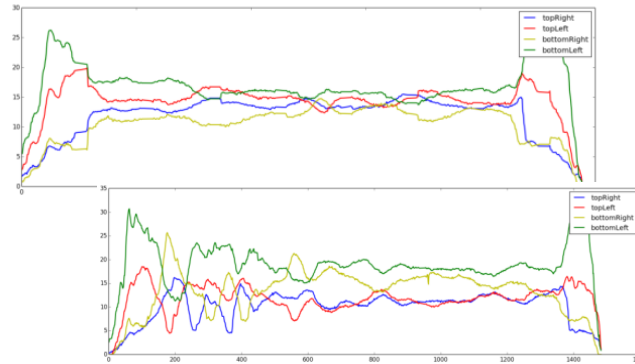
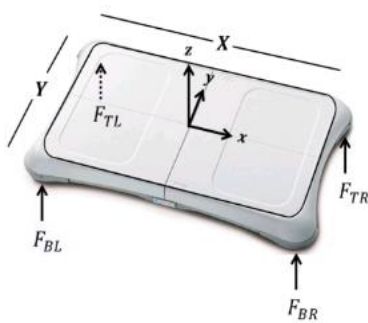
Dataset is available online on the UCI repository

<http://archive.ics.uci.edu/ml/datasets/Activity+Recognition+system+based+on+Multisensor+data+fusion+%28AReM%29>

Clinical applications

- Automatic assessment of balance skills
- Predict the outcome of the Berg Balance Scale (BBS) clinical test from time-series of pressure sensors

Wii
Balance
Board

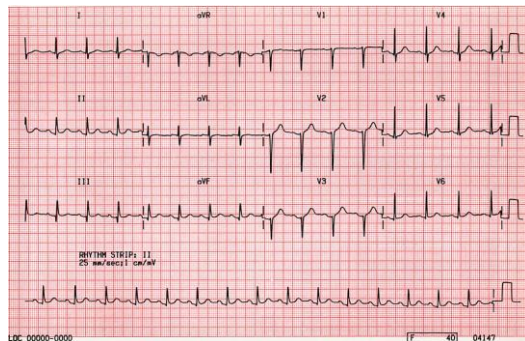


BBS

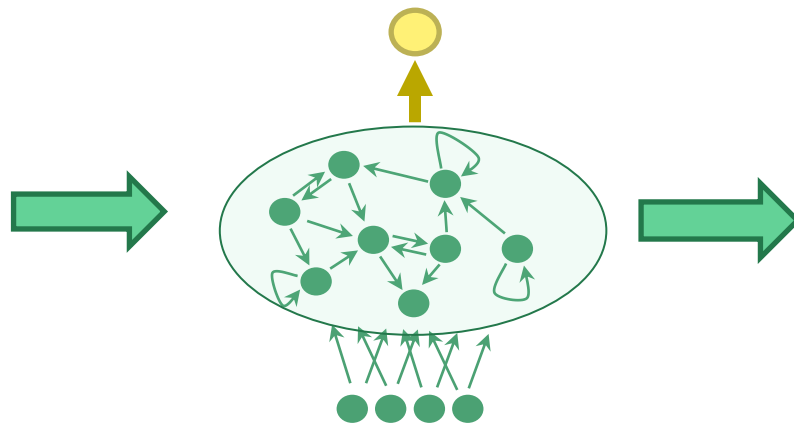


Brugada Syndrome

Dimitri, Giovanna Maria, et al. "A preliminary evaluation of Echo State Networks for Brugada syndrome classification." SSCI, IEEE, 2021.



ECG leads in input



processed by ESNs

Brugada Type 1
syndrome diagnosis
 $\approx 80\%$ accurate

TEACHING

A computing Toolkit for building Efficient Autonomous applications leveraging Humanistic INtelligence is an EU-funded project that designs a computing platform and the associated software toolkit supporting the development and deployment of autonomous, adaptive and dependable CPSoS applications, allowing them to exploit a sustainable human feedback to drive, optimize and personalize the provisioning of their services.

<https://www.teaching-h2020.eu>



https://twitter.com/TEACHING_H2020



<https://www.linkedin.com/company/teaching-horizon-2020/>

RC in Autonomous Vehicles

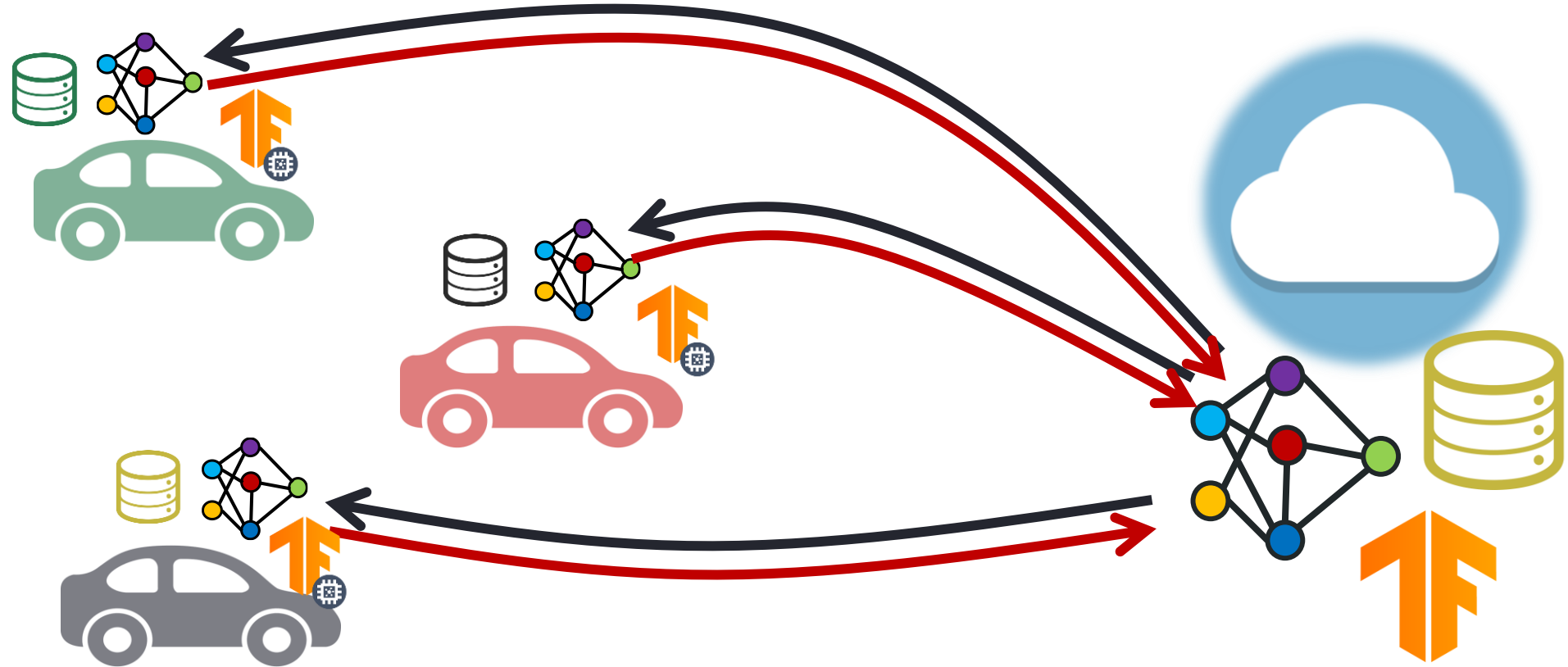
- Automatic detection of physiological, emotional, cognitive state of the human → **Human-centric personalization**
- **Good performance in human state monitoring + efficiency**

	WESAD		HHAR		PAMAP2		OPPORTUN.		ASCERTAIN	
	Avg	Std	Avg	Std	Avg	Std	Avg	Std	Avg	Std
RNN	94.62	2.84	78.54	2.04	96.00	3.39	96.84	2.58	94.77	0.78
ESN	94.96	2.60	89.79	3.81	97.50	2.74	94.74	5.77	96.54	0.77
LSTM	95.48	1.17	92.71	2.72	96.50	1.22	93.08	2.88	94.63	0.00
GRU	98.13	1.16	98.54	0.83	98.50	2.00	96.84	2.58	94.63	0.00

D. Bacciu, D. Di Sarli, C. Gallicchio, A. Micheli, N. Puccinelli, "Benchmarking Reservoir and Recurrent Neural Networks for Human State and Activity Recognition", IWANN 2021

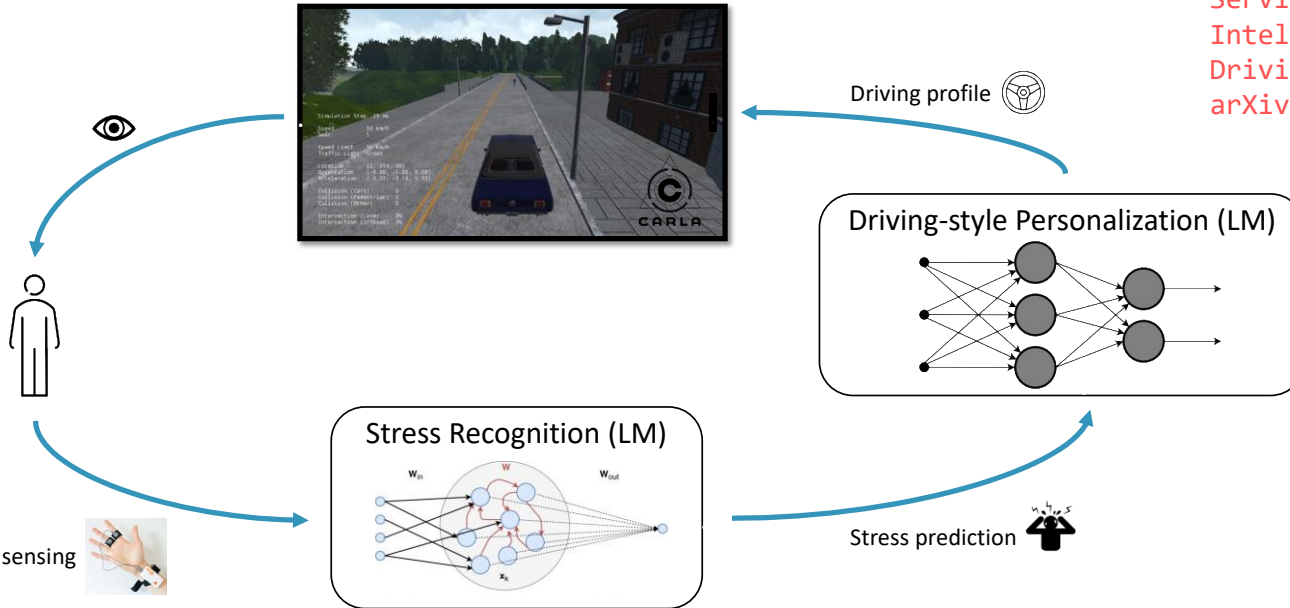


Distributed, embeddable and federated learning

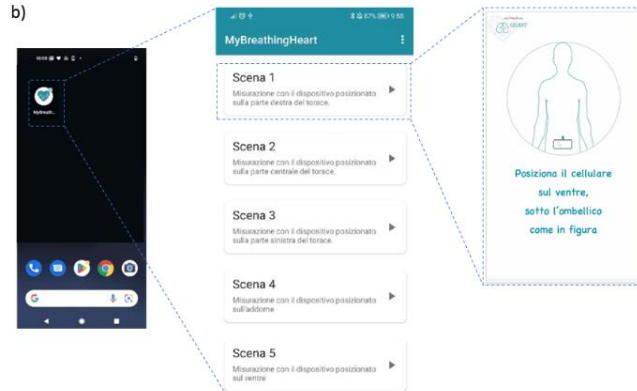
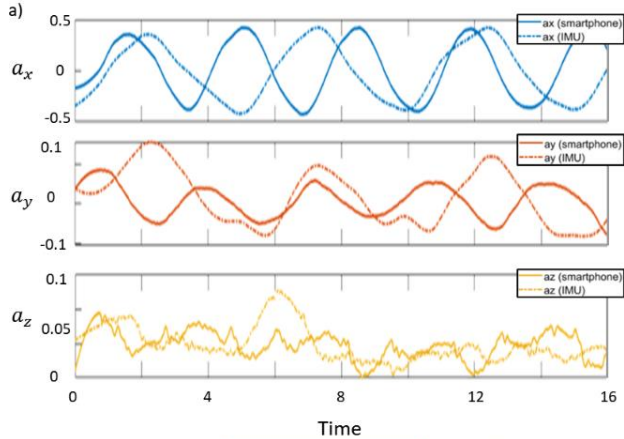


Driving-Style Personalization Based on Driver Stress

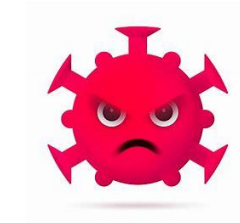
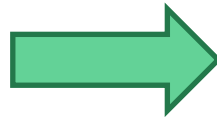
De Caro, Valerio, et al. "AI-as-a-Service Toolkit for Human-Centered Intelligence in Autonomous Driving." arXiv preprint arXiv:2202.01645, PERCOM 2022



MyBreathingHeart



Sviluppo ed implementazione di un'applicazione per smartphone per il monitoraggio remoto di problemi cardio-respiratori durante crisi pandemica



EMERGE

<https://eic-emerge.eu>

The image shows a screenshot of the EMERGE website homepage. The background is a dark blue space with a grid of small, glowing dots in various colors (blue, red, yellow) and some faint, curved lines. In the top left corner, the word "EMERGE" is written in a light blue, sans-serif font. In the top right corner, there is a navigation menu with the following items: "Home", "About", "Consortium", "Resources", "Outreach", and "Contact", all in a light blue font. The main content area features a large, white, sans-serif title "Emergent Awareness from Minimal Collectives". Below the title, there is a paragraph of white text that reads: "How do robots in a collective know what the group as a whole is doing? How can connected devices make sense of the world around them with so many interconnections? How can a robotic arm composed of many independent parts understand how its body is behaving as it reaches for an object?". In the bottom right corner, there are several overlapping squares of different shades of gray and white, some with small white dots inside them.

Reservoir Computing: Research

Quality of Reservoir dynamics

- **Entropy** of recurrent units activations
 - Unsupervised adaptation of reservoirs using Intrinsic Plasticity
- Study the **short-term memory ability** of the system
 - Memory Capacity and relations to linearity
- **Edge of stability/chaos**: reservoir at the border of stability
 - Recurrent systems close to instability show optimal performances whenever the task at hand requires long short-term memory

Intrinsic Plasticity

- Adapt gain and bias of the act. function
- Tune the probability density of reservoir neurons to maximum entropy

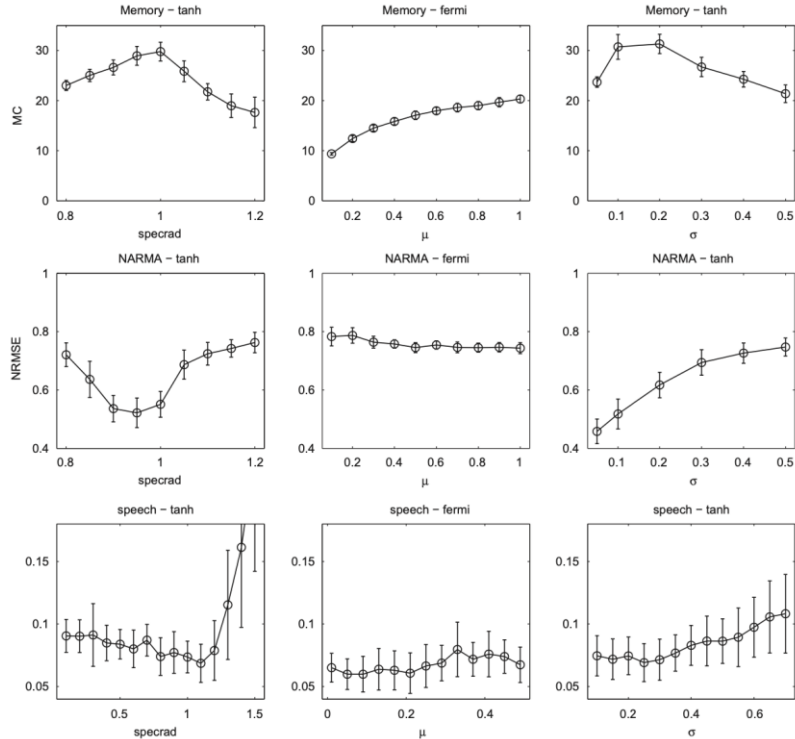


Fig. 4. Results for all three benchmarks for tanh with spectral radius ranging (left column), exponential IP for fermi nodes (middle column), and Gaussian IP for tanh nodes (right column).

$$f_{\text{gen}}(x) = f(ax + b)$$

$$\Delta b = -\eta \left(-\frac{\mu}{\sigma^2} + \frac{y}{\sigma^2} (2\sigma^2 + 1 - y^2 + \mu y) \right),$$

$$\Delta a = \frac{\eta}{a} + \Delta b x.$$

Schrauwen, B., Wardermann, M., Verstraeten, D., Steil, J.J. and Stroobandt, D., 2008. Improving reservoirs using intrinsic plasticity. *Neurocomputing*, 71(7-9), pp.1159-1171.

Edge of chaos

Improved dynamics near the transition between ordered and chaotic

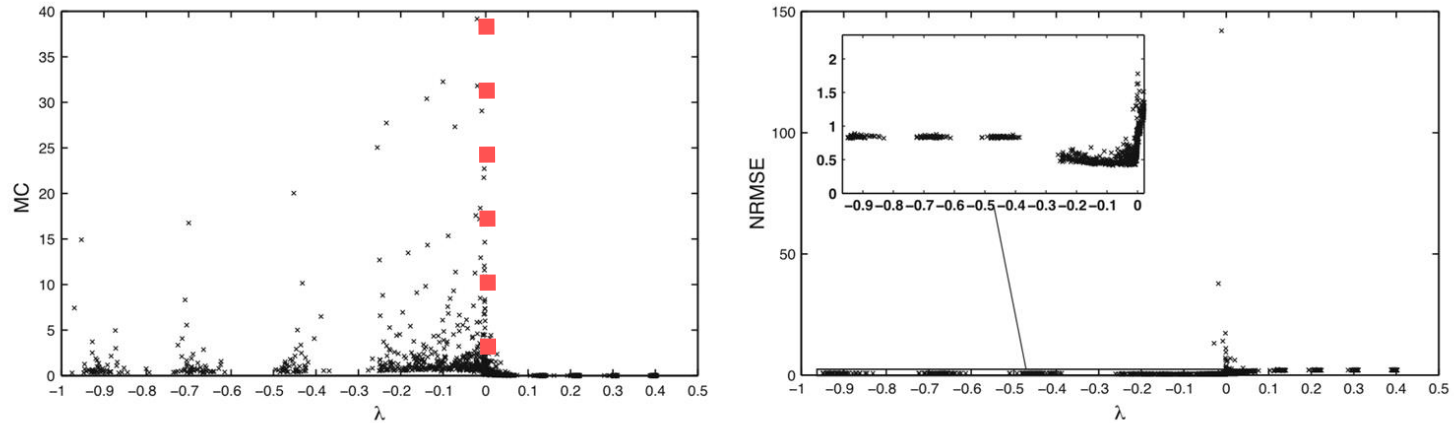
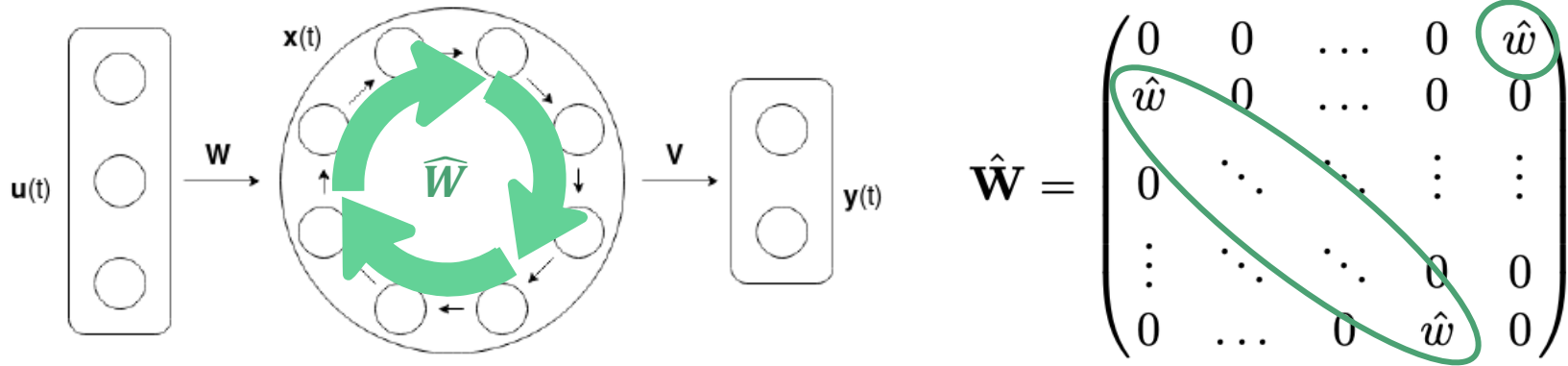


Fig. 3 *Left* Memory capacity versus estimated Lyapunov exponent. *Right* Normalized root mean squared error (NRMSE) versus estimated Lyapunov exponent

Simple Cycle Reservoir (SCR)

The reservoir layer has an easy-to-build orthogonal structure



Rodan, A. and Tino, P., 2010. Minimum complexity echo state network. IEEE transactions on neural networks, 22(1), pp.131-144.

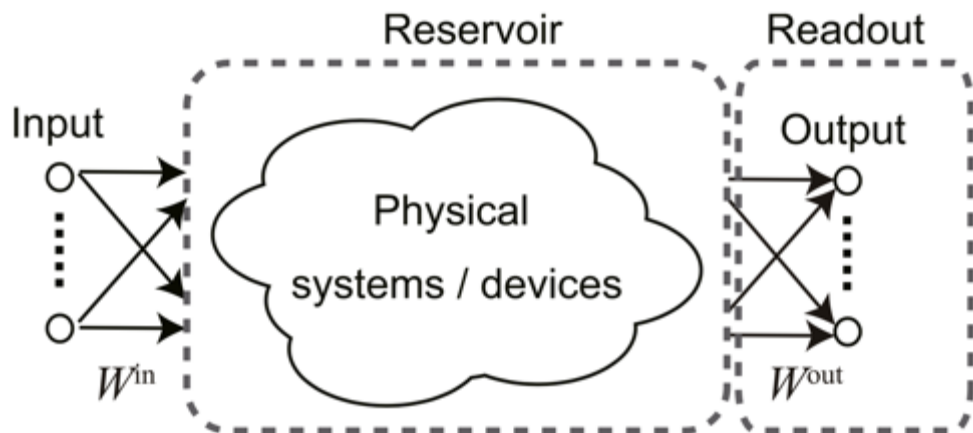
Approximation Capabilities

- Echo State Networks can approximate any fading memory filter
- non-linear reservoir + linear readout
- trigonometric state affine reservoir systems + linear readout
- linear reservoir systems + non-linear readout (e.g., MLP)

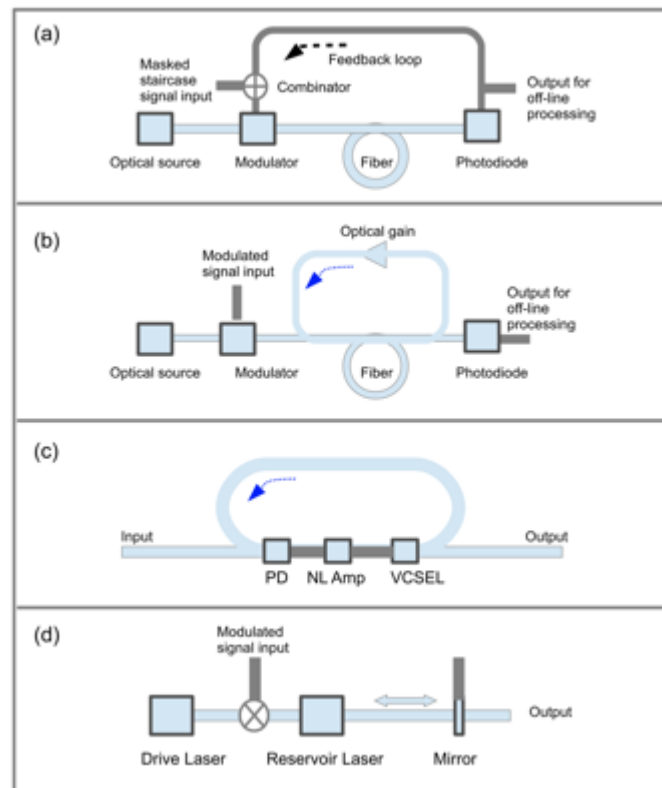
Lyudmila Grigoryeva and Juan-Pablo Ortega. Echo state networks are universal. *Neural Networks*, 108:495–508, 2018.

Lukas Gonon and Juan-Pablo Ortega. Reservoir computing universality with stochastic inputs. *IEEE transactions on neural networks and learning systems*, 2019

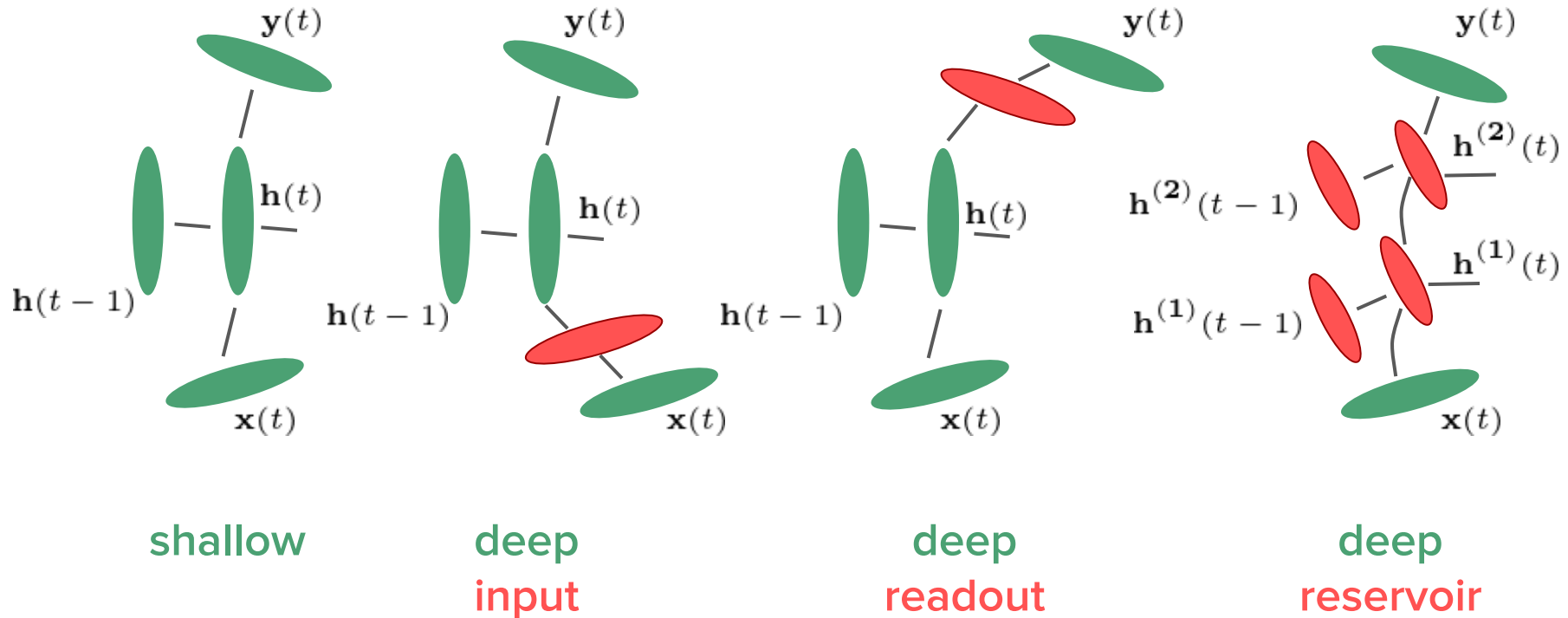
Physical Reservoir Computing



Tanaka, G., Yamane, T., Héroux, J.B., Nakane, R., Kanazawa, N., Takeda, S., Numata, H., Nakano, D. and Hirose, A., 2019. Recent advances in physical reservoir computing: A review. *Neural Networks*, 115, pp.100-123.

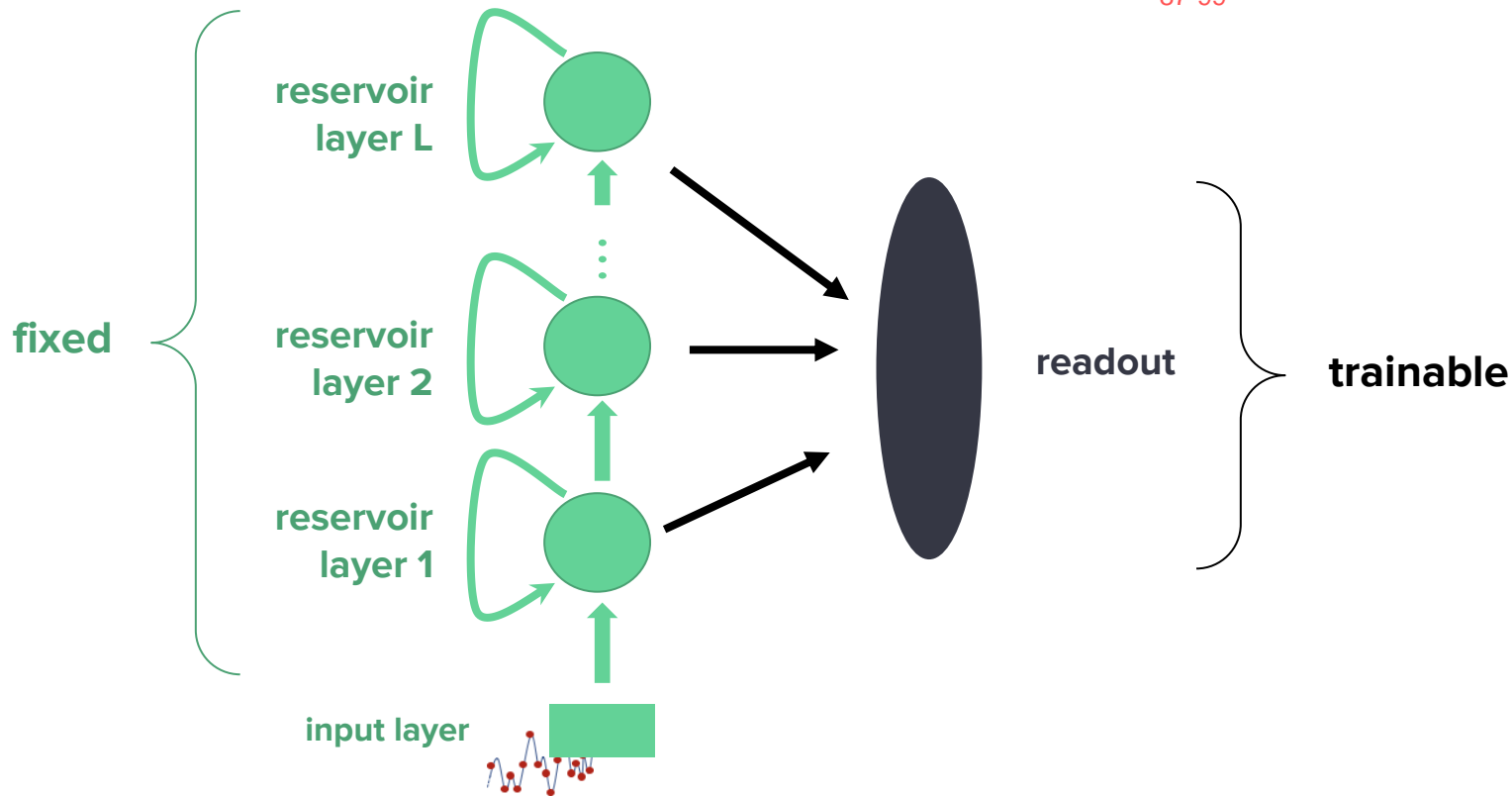


Depth in RNNs



Deep Echo State Networks

Gallicchio, Claudio, Alessio Micheli, and Luca Pedrelli. "Deep reservoir computing: A critical experimental analysis." *Neurocomputing* 268 (2017): 87-99



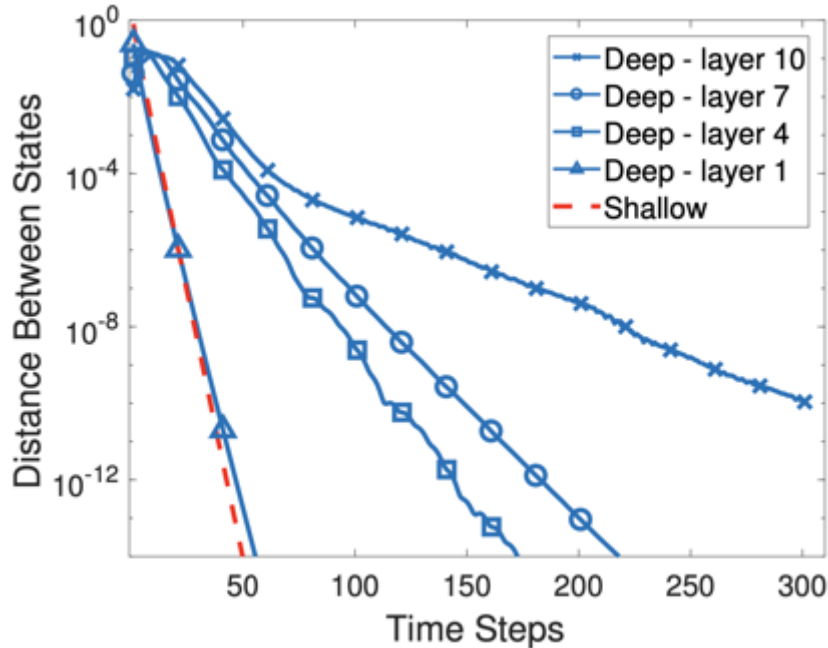
Deep Echo State Networks

Deep reservoir = nested set of dynamical systems

$$\begin{aligned} \boxed{\mathbf{h}^{(L)}(t)} &= \tanh(\mathbf{W}^{(L)}) \boxed{\mathbf{h}^{(L-1)}(t)} + \mathbf{W}_R^{(L)} \mathbf{h}^{(L)}(t-1) \\ &\quad \vdots \\ \boxed{\mathbf{h}^{(2)}(t)} &= \tanh(\mathbf{W}^{(2)}) \boxed{\mathbf{h}^{(1)}(t)} + \mathbf{W}_R^{(2)} \mathbf{h}^{(2)}(t-1) \\ \boxed{\mathbf{h}^{(1)}(t)} &= \tanh(\mathbf{W}^{(1)}) \boxed{\mathbf{x}(t)} + \mathbf{W}_R^{(1)} \mathbf{h}^{(1)}(t-1) \end{aligned}$$

Gallicchio, Claudio, Alessio Micheli, and Luca Pedrelli. "Deep reservoir computing: A critical experimental analysis." *Neurocomputing* 268 (2017): 87-99

Multiple time-scales

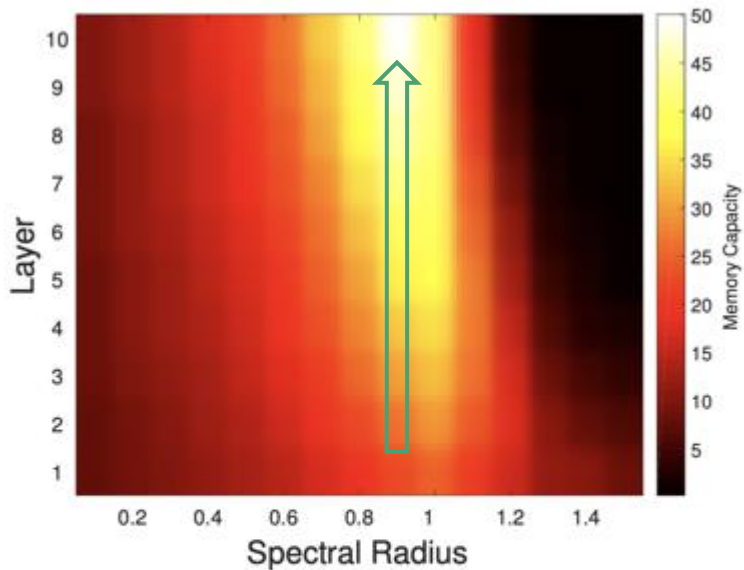


- Effects of input perturbations last longer in the higher reservoir layers
- Multiple time-scales representation is intrinsic

Galicchio, Claudio, Alessio Micheli, and Luca Pedrelli. "Deep reservoir computing: A critical experimental analysis." *Neurocomputing* 268 (2017): 87-99

Galicchio, C. and Micheli, A., 2018, July. Why Layering in Recurrent Neural Networks? A DeepESN Survey. In 2018 International Joint Conference on Neural Networks (IJCNN)(pp. 1-8). IEEE.

Richer dynamics: short-term memory



Galicchio, C. and Micheli, A., 2018, July. Why Layering in Recurrent Neural Networks? A DeepESN Survey. In 2018 International Joint Conference on Neural Networks (IJCNN)(pp. 1-8). IEEE.

Fig. 7. Averaged Memory Capacity of individual layers of DeepESN, shown for increasing values of the spectral radius, as computed in [49]. Results correspond to a DeepESN setting in which each layer comprises a number of 100 recurrent reservoir units. Differently from the results in Figure 6, Memory Capacity in this plot refers to reservoir-readout connections that are trained separately for each layer. Further details and results can be found in [49].

Richer dynamics: stability regime

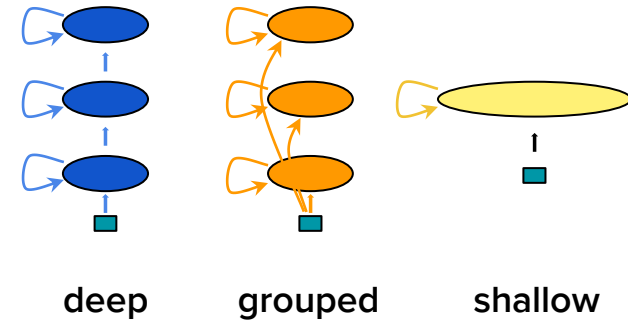
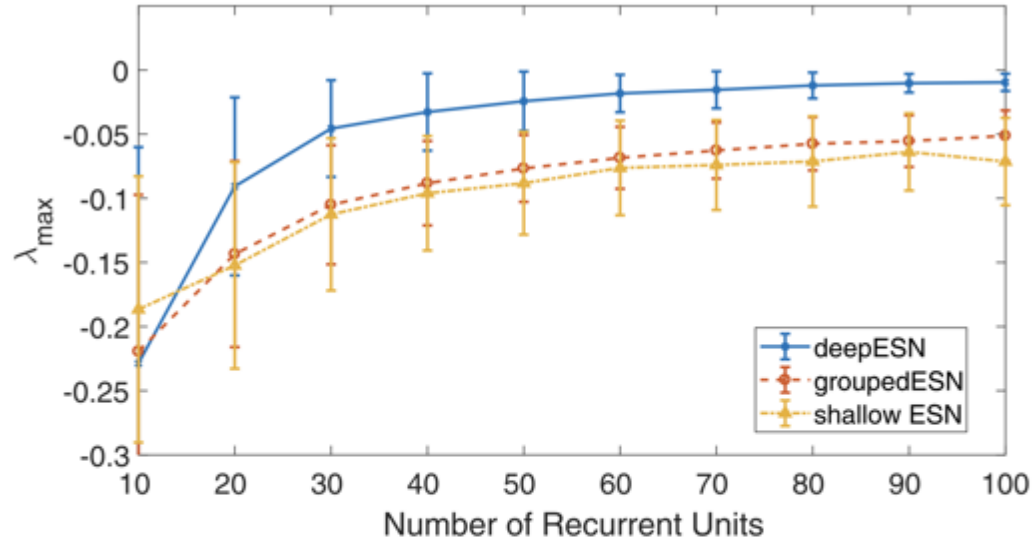
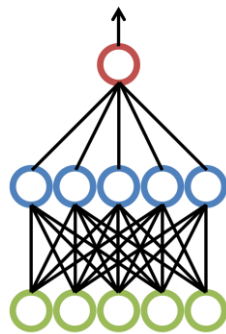
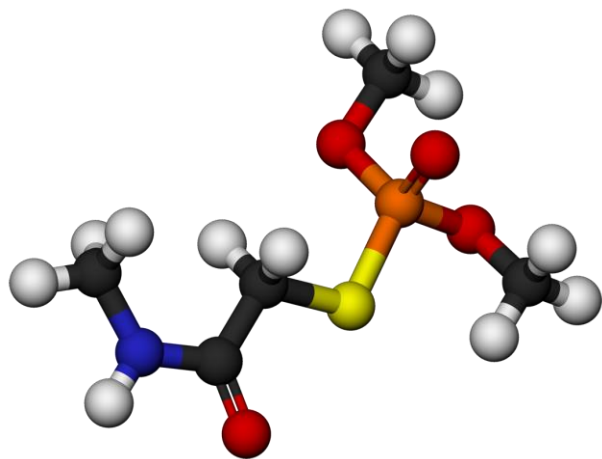


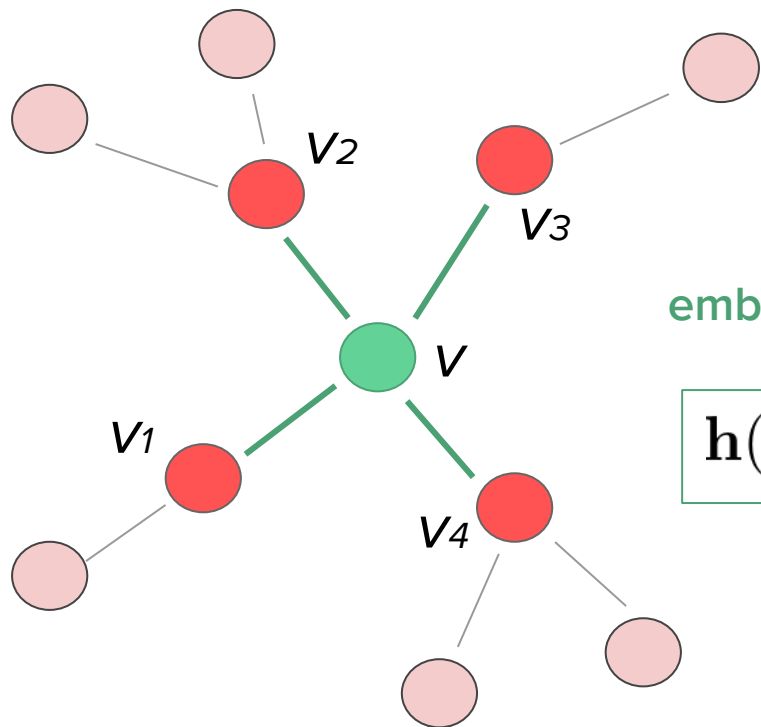
Fig. 4. Averaged values of λ_{max} obtained by DeepESN for increasing number of reservoir units, organized in layers of 10 units each. The considered hyper-parameterization corresponds to $\rho = 1$, $a = 1$, $scale_{in} = 1$ and $scale_{il} = 0.5$. Results achieved by a shallow ESN and groupedESN with the same hyper-parameterization and the same number of reservoir units are reported as well for the sake of comparison.

Gallicchio, C., Micheli, A. and Silvestri, L., 2018. Local Lyapunov exponents of deep echo state networks. *Neurocomputing*, 298, pp.34-45.

Neural networks for graphs



Vertex-wise graph encoding



- time-step \rightarrow vertex
- previous time step \rightarrow neighborhood

embedding (state)

$$\mathbf{h}(v) = \tanh(\mathbf{W} \mathbf{x}(v)) + \sum_{v' \in \mathcal{N}(v)} \mathbf{W}_R \mathbf{h}(v')$$

input features

embeddings of neighbors

Reservoir Computing for graphs

$$\mathbf{H} = \tanh \left(\mathbf{W}\mathbf{X} + \mathbf{W}_R\mathbf{H}\tilde{\mathbf{A}} \right)$$

- **Basic idea:** encode the input graph as the fixed point of a dynamical system
- Impose stability of the iterated map - Graph Embedding Stability (GES)
 - E.g., $\rho(\mathbf{W}_R) < 1$

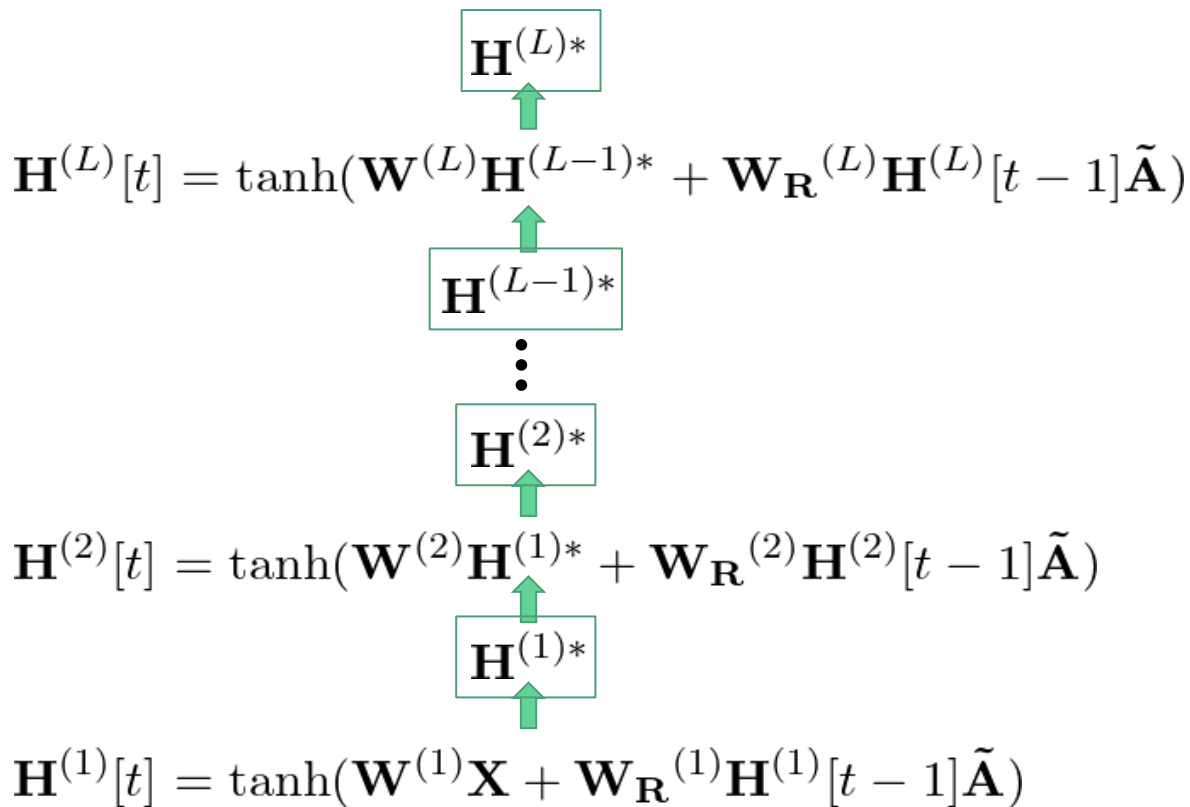
Reservoir Layer for graphs

$$\mathbf{H}[t] = \tanh(\mathbf{W}\mathbf{X} + \mathbf{W}_R\mathbf{H}[t-1]\tilde{\mathbf{A}})$$

- Initialize randomly under the GES condition
- For each graph in your dataset:
 1. Initialize $\mathbf{H}[0]$ (e.g., to $\mathbf{0}$)
 2. Iterate the above equation until convergence

Gallicchio, C. and Micheli, A., 2020. Fast and Deep Graph Neural Networks. In AAAI (pp. 3898-3905).

Fast and Deep Graph Neural Networks (FDGNN)



Galicchio, C. and Micheli, A.,
2020. Fast and Deep Graph
Neural Networks. In AAAI (pp.
3898-3905).

It's accurate

Galicchio, C. and Micheli, A., 2020. Fast and Deep Graph Neural Networks. In AAAI (pp. 3898-3905).

	MUTAG	PTC	COX2	PROTEINS	NCI1
FDGNN	88.51 ± 3.77	63.43 ± 5.35	83.39 ± 2.88	76.77 ± 2.86	77.81 ± 1.62
FDGNN _(L=1)	87.38 ± 6.55	63.43 ± 5.35	82.41 ± 2.67	76.77 ± 2.86	77.11 ± 1.52
GNN (Uwents et al. 2011)	80.49 ± 0.81	-	-	-	-
RelNN (Uwents et al. 2011)	87.77 ± 2.48	-	-	-	-
DGCNN (Zhang et al. 2018)	85.83 ± 1.66	58.59 ± 2.47	-	75.54 ± 0.94	74.44 ± 0.47
PGC-DGCNN (Tran, Navarin, and Sperduti 2018)	87.22 ± 1.43	61.06 ± 1.83	-	76.45 ± 1.02	76.13 ± 0.73
DCNN (Tran, Navarin, and Sperduti 2018)	-	-	-	61.29 ± 1.60	56.61 ± 1.04
PSCN (Tran, Navarin, and Sperduti 2018)	-	-	-	75.00 ± 2.51	76.34 ± 1.68
GK (Zhang et al. 2018)	81.39 ± 1.74	55.65 ± 0.46	-	71.39 ± 0.31	62.49 ± 0.27
DGK (Yanardag and Vishwanathan 2015)	82.66 ± 1.45	57.32 ± 1.13	-	71.68 ± 0.50	62.48 ± 0.25
RW (Zhang et al. 2018)	79.17 ± 2.07	55.91 ± 0.32	-	59.57 ± 0.09	-
PK (Zhang et al. 2018)	76.00 ± 2.69	59.50 ± 2.44	81.00 ± 0.20	73.68 ± 0.68	82.54 ± 0.47
WL (Zhang et al. 2018)	84.11 ± 1.91	57.97 ± 2.49	83.20 ± 0.20	74.68 ± 0.49	84.46 ± 0.45
KCNN (Nikolentzos et al. 2018)	-	62.94 ± 1.69	-	75.76 ± 0.28	77.21 ± 0.22
CGMM (Bacciu, Errica, and Micheli 2018)	85.30	-	-	-	-

It's accurate

Galicchio, C. and Micheli, A., 2020. Fast and Deep Graph Neural Networks. In AAI (pp. 3898-3905).

	IMDB-b	IMDB-m	REDDIT	COLLAB
FDGNN	72.36 ± 3.63	50.03 ± 1.25	89.48 ± 1.00	74.44 ± 2.02
FDGNN _(L=1)	71.79 ± 3.37	49.34 ± 1.70	87.74 ± 1.61	73.82 ± 2.32
DGCNN (Zhang et al. 2018)	70.03 ± 0.86	47.83 ± 0.85	-	73.76 ± 0.49
PGC-DGCNN (Tran, Navarin, and Sperduti 2018)	71.62 ± 1.22	47.25 ± 1.44	-	75.00 ± 0.58
PSCN (Tran, Navarin, and Sperduti 2018)	71.00 ± 2.29	45.23 ± 2.84	-	72.60 ± 2.15
GK (Yanardag and Vishwanathan 2015)	65.87 ± 0.98	43.89 ± 0.38	77.34 ± 0.18	72.84 ± 0.56
DGK (Yanardag and Vishwanathan 2015)	66.96 ± 0.56	44.55 ± 0.52	78.04 ± 0.39	73.09 ± 0.25
KCNN (Nikolentzos et al. 2018)	71.45 ± 0.15	47.46 ± 0.21	81.85 ± 0.12	74.93 ± 0.14

It's fast

Table 3: Running times required by FDGNN (in single core mode, without GPU acceleration). Results are averaged (and std are computed) on the outer 10 folds.

Task	Training	Test
MUTAG	0.56'' \pm 0.33	0.06'' \pm 0.04
PTC	0.16'' \pm 0.03	0.02'' \pm 0.00
COX2	1.36'' \pm 0.42	0.15'' \pm 0.05
PROTEINS	2.16'' \pm 0.47	0.24'' \pm 0.04
NCI1	2.00'' \pm 0.45	13.36'' \pm 3.02
IMDB-b	7.46'' \pm 3.14	0.83'' \pm 0.35
IMDB-m	8.68'' \pm 1.73	0.98'' \pm 0.22
REDDIT	2.47'' \pm 0.01	16.49'' \pm 0.28
COLLAB	22.86'' \pm 4.70	2.54'' \pm 0.52

Table 4: Comparison of training times required on MUTAG by FDGNN, GNN, GIN and WL. Results are averaged (and std are computed) on the outer 10 folds.

FDGNN	GNN	GIN	WL
0.56''\pm0.33	202.28'' \pm 166.87	499.24'' \pm 2.25	1.16'' \pm 0.03

Reservoir Computing by discretizing ODEs

- Euler State Networks (EuSN)

- stable dynamics + non-dissipation of the input over time

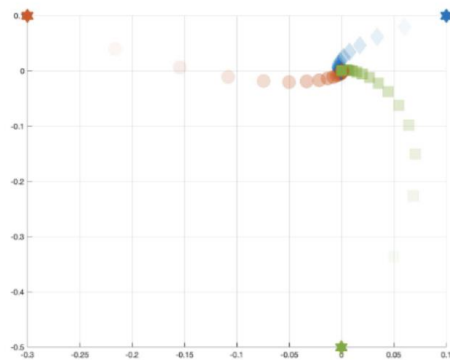
$$h' = \tanh(W_x x + W_h h + b)$$

1. impose antisymmetric recurrent weight matrix to enforce critical dynamics
2. discretize the ODE

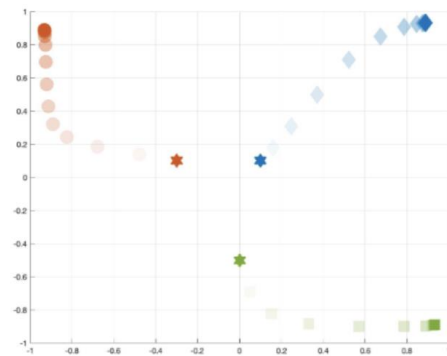
$$h_t = h_{t-1} + \underbrace{\epsilon}_{\text{step size}} \tanh(W_x x_t + (W_h - W_h^T - \underbrace{\gamma I}_{\text{diffusion coefficient}}) h_{t-1} + b)$$

The input signal is preserved without exploding nor dying

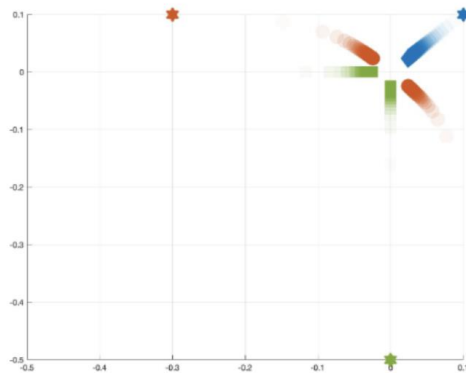
Gallicchio, Claudio. "Euler State Networks." arXiv preprint arXiv:2203.09382 (2022).



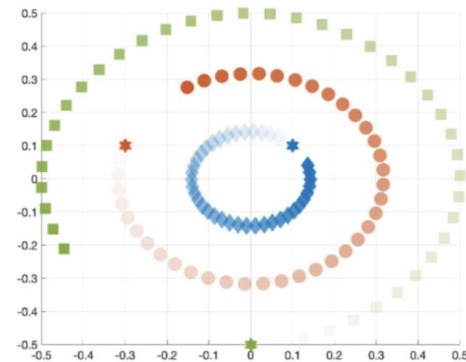
(a) ESN with ESP.



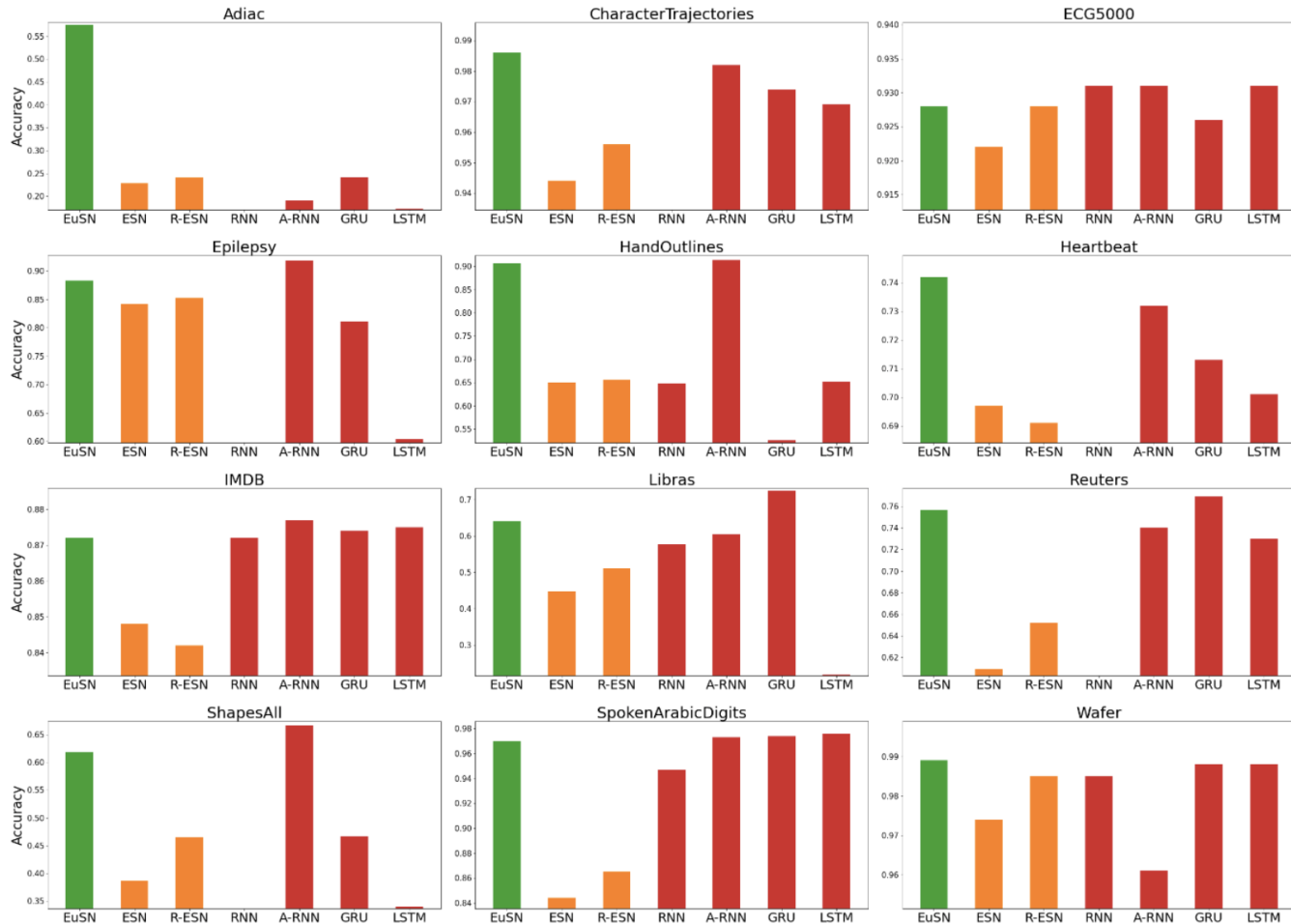
(b) ESN without ESP.



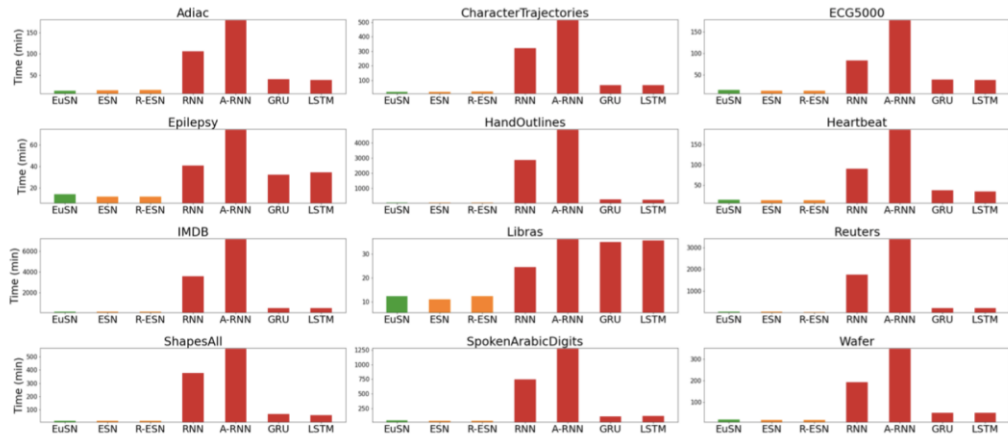
(c) R-ESN.



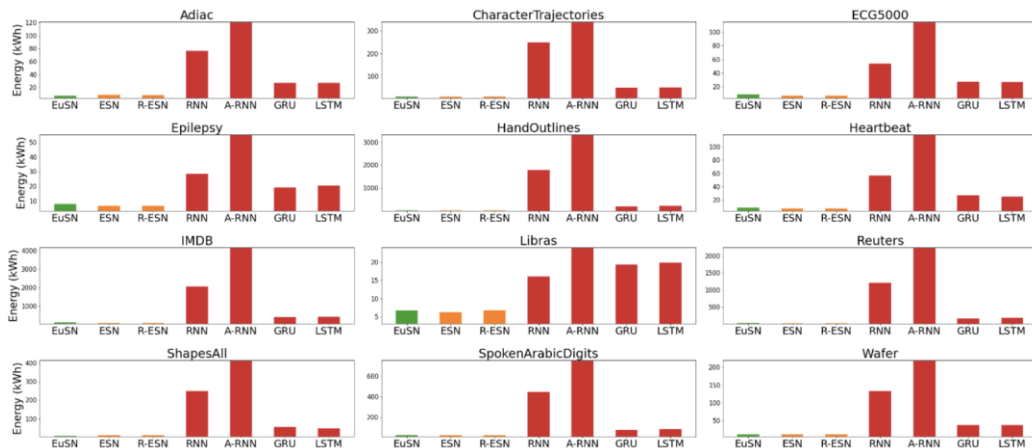
(d) EuSN.



High accuracy vs
state-of-the-art
fully trainable
models & ESNs



Extremely more efficient (up to 100x) than fully trainable models



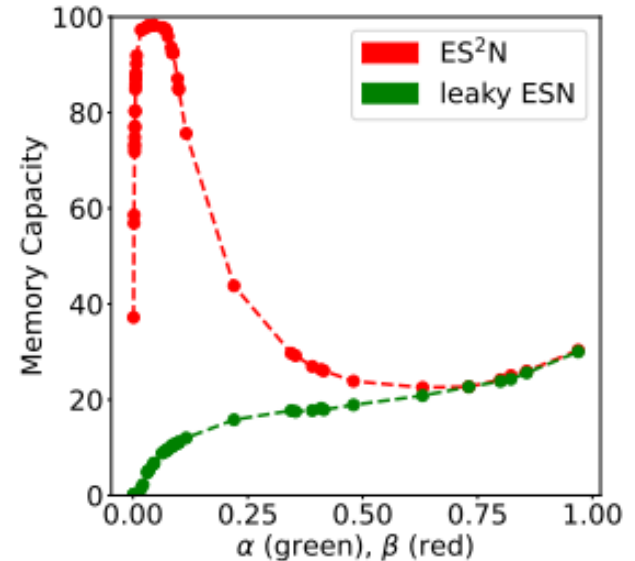
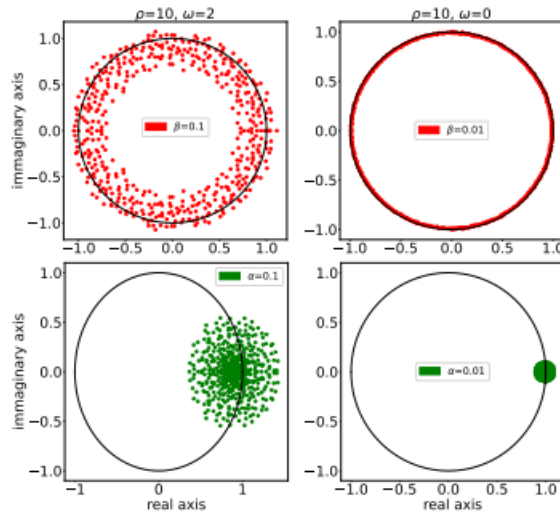
Edge of Stability Reservoir Computing

Put a random orthogonal matrix here transforming the hidden state

$$\mathbf{h}_t = (1 - \alpha)\mathbf{h}_{t-1} + \alpha \tanh(\mathbf{x}_t \mathbf{W}_{xh} + \mathbf{h}_{t-1} \mathbf{W}_{hh}) \quad \text{Leaky ESN}$$

$$\mathbf{h}_t = (1 - \beta) \mathbf{O} \mathbf{h}_{t-1} + \beta \tanh(\mathbf{x}_t \mathbf{W}_{xh} + \mathbf{h}_{t-1} \mathbf{W}_{hh}) \quad \text{ES}^2\text{N}$$

Ceni, Andrea, and Claudio Gallicchio. "Edge of stability echo state networks." *arXiv preprint arXiv:2308.02902* (2023).

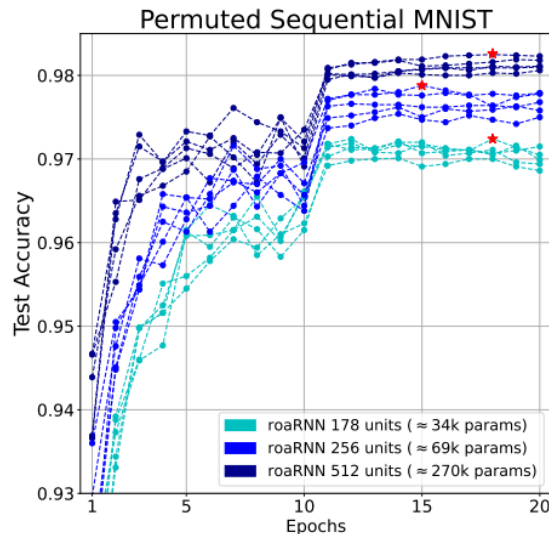


RoarRNN: fully trained ESESNN

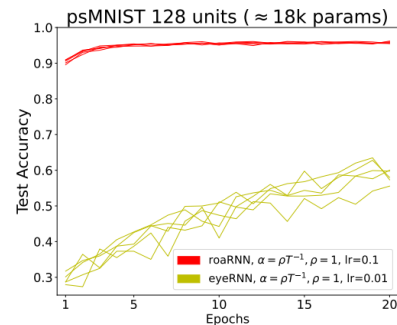
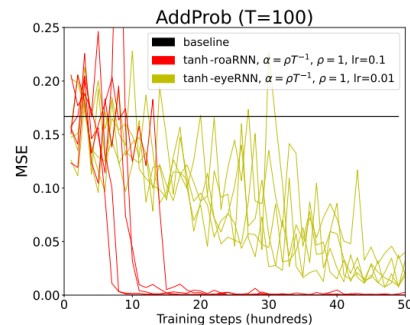
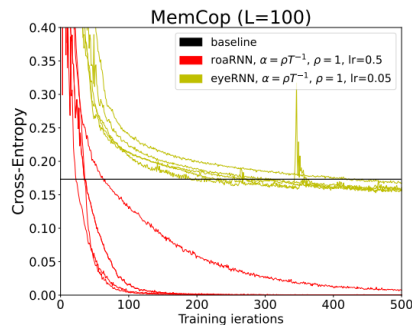
A simple solution to the V/E gradient issue!

Ceni, Andrea. "Random orthogonal additive filters: a solution to the vanishing/exploding gradient of deep neural networks." *arXiv preprint arXiv:2210.01245* (2022).

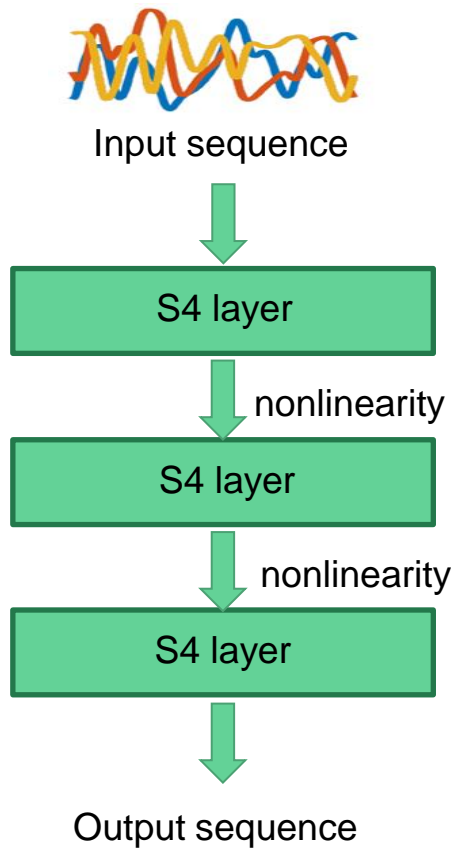
The identity in place of a random orthogonal matrix doesn't give same results!



Model	Parameters	Test accuracy
Vanilla RNN [46]	≈68k	71.6%
LSTM [31]	≈270k	92.9%
GRU [46]	≈200k	94.1%
Dilated CNN [46]	≈46k	96.7%
FC uRNN [29]	≈270k	94.1%
BN LSTM [57]	—	95.4%
expRNN [30]	≈137k	96.6%
Lipschitz RNN [42]	≈ 34k	96.3%
res-IndRNN [56]	—	97.02%
dense-IndRNN [56]	—	97.2%
Shuffling RNN [40]	≈50k	96.43%
NRU [45]	≈165k	95.38%
LMU [44]	≈102k	97.15%
coRNN [43]	≈134k	97.3%
roaRNN	≈ 34k	97.24%
roaRNN	≈ 69k	97.88%
roaRNN	≈270k	98.25%



STATE SPACE MODELS



$$\begin{aligned} x'(t) &= \mathbf{A}x(t) + \mathbf{B}u(t) \\ y(t) &= \mathbf{C}x(t) + \mathbf{D}u(t) \end{aligned}$$

$$u_k = u(k\Delta)$$

discretisation

$$\begin{aligned} x_k &= \overline{\mathbf{A}}x_{k-1} + \overline{\mathbf{B}}u_k \\ y_k &= \overline{\mathbf{C}}x_k \end{aligned}$$

Gu, Albert, Karan Goel, and Christopher Ré.
 "Efficiently modeling long sequences with structured
 state spaces." *arXiv preprint arXiv:2111.00396* (2021).

Unfold
in time

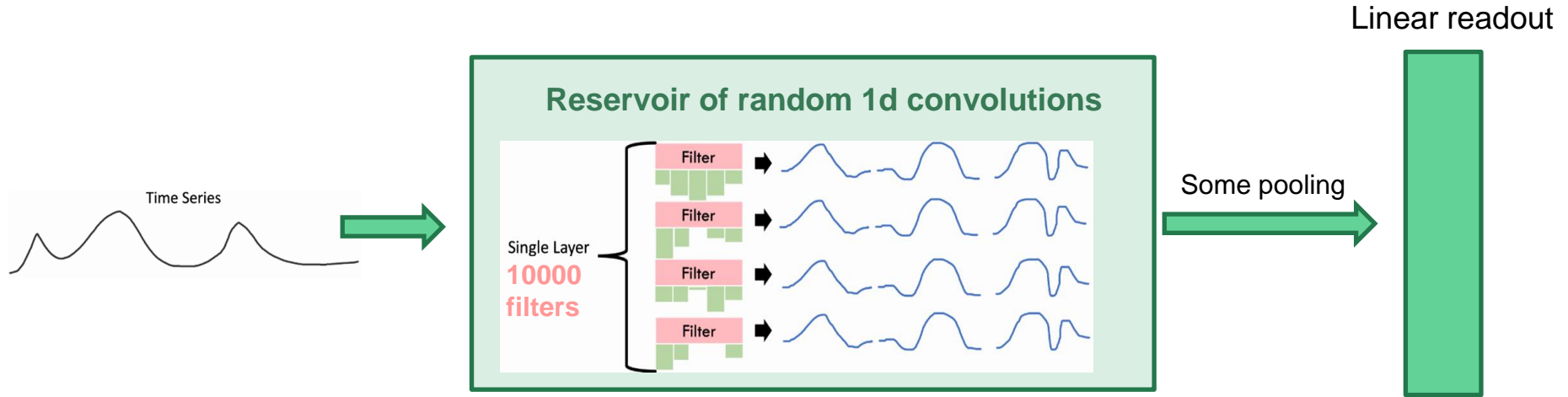
$$y_k = \overline{\mathbf{C}}\mathbf{A}^k\overline{\mathbf{B}}u_0 + \overline{\mathbf{C}}\mathbf{A}^{k-1}\overline{\mathbf{B}}u_1 + \dots + \overline{\mathbf{C}}\mathbf{A}\overline{\mathbf{B}}u_{k-1} + \overline{\mathbf{C}}\overline{\mathbf{B}}u_k$$

$$y = \overline{\mathbf{K}} * u.$$

Convolutional representation

$$\overline{\mathbf{K}} \in \mathbb{R}^L := \mathcal{K}_L(\overline{\mathbf{A}}, \overline{\mathbf{B}}, \overline{\mathbf{C}}) := \left(\overline{\mathbf{C}}\mathbf{A}^i\overline{\mathbf{B}} \right)_{i \in [L]} = (\overline{\mathbf{C}}\overline{\mathbf{B}}, \overline{\mathbf{C}}\mathbf{A}\overline{\mathbf{B}}, \dots, \overline{\mathbf{C}}\mathbf{A}^{L-1}\overline{\mathbf{B}}).$$

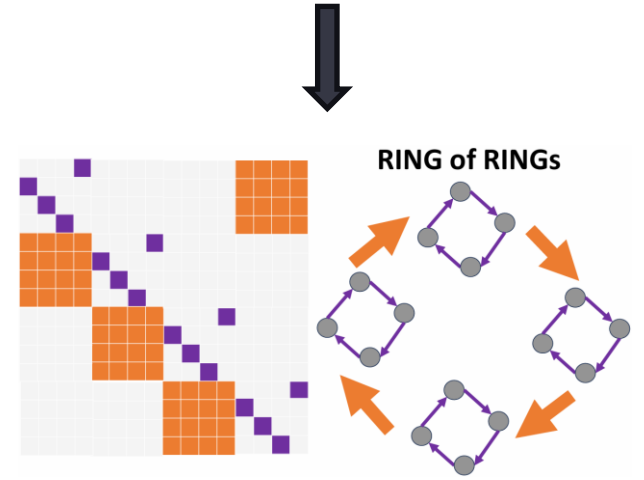
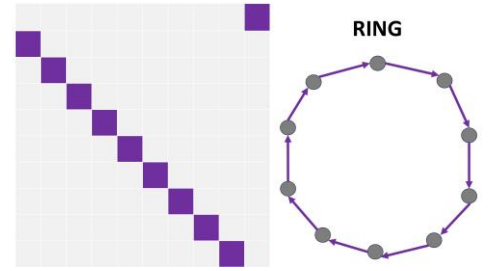
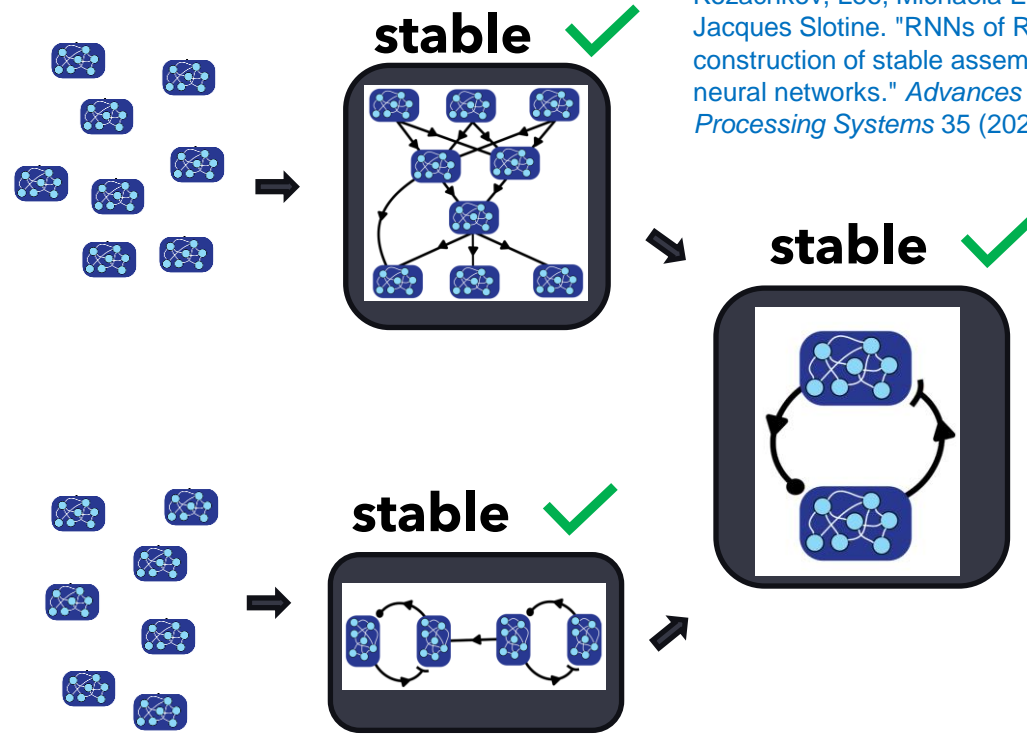
ROCKET



Dempster, Angus, François Petitjean, and Geoffrey I. Webb. "ROCKET: exceptionally fast and accurate time series classification using random convolutional kernels." *Data Mining and Knowledge Discovery* 34.5 (2020): 1454-1495.

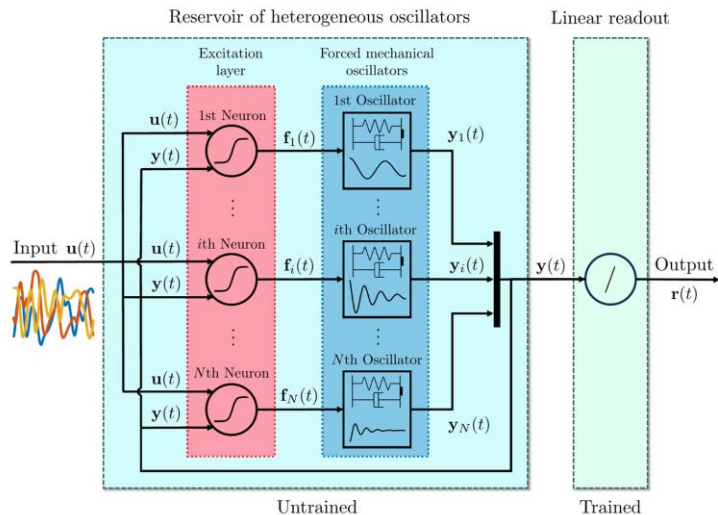
MODULAR COMPOSITION of RNNs

Kozachkov, Leo, Michaela Ennis, and Jean-Jacques Slotine. "RNNs of RNNs: Recursive construction of stable assemblies of recurrent neural networks." *Advances in Neural Information Processing Systems* 35 (2022): 30512-30527.



RANDOM OSCILLATORS NETWORK

Ceni, Andrea, et al. "Random Oscillators Network for Time Series Processing." *International Conference on Artificial Intelligence and Statistics*. PMLR, 2024.

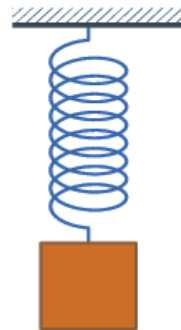


Reservoir of oscillators equation

$$\ddot{\mathbf{y}} = \tanh(\mathbf{W}\mathbf{y} + \mathbf{V}\mathbf{u}(t) + \mathbf{b}) - \gamma \odot \mathbf{y} - \varepsilon \odot \dot{\mathbf{y}}$$

Linear readout:

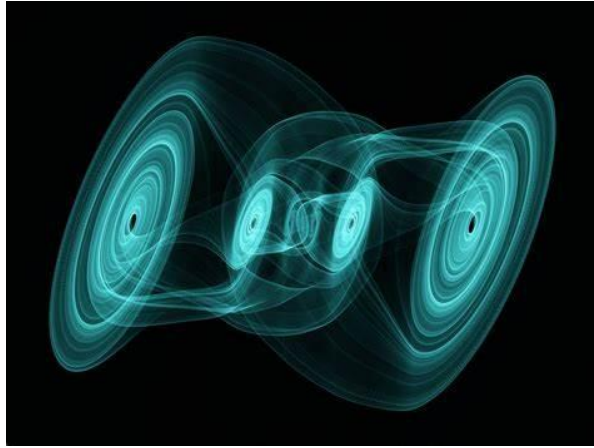
$$\mathbf{r} = \mathbf{W}_o \mathbf{y} + \mathbf{b}_o$$



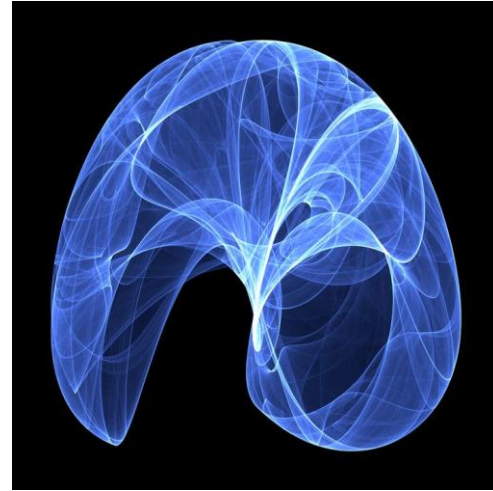
Model	Fully-trained			Randomised	
	LSTM	coRNN	hcoRNN (our)	Leaky ESN	RON (our)
sMNIST ↑	0.9860 0.0017	0.9921 0.0002	0.9871 0.0011	0.9211 0.0020	0.9780 0.0006
psMNIST ↑	0.8761 0.0390	0.9435 0.0224	0.9635 0.0048	0.8503 0.0150	0.9301 0.0054
npCIFAR-10 ↑	0.1000 0.0000	0.5841 0.0033	0.5548 0.0031	0.2060 0.0016	0.4158 0.0101
FordA ↑	0.5803 0.0432	0.7003 0.1535	0.7944 0.0859	0.5461 0.0320	0.6885 0.0385
Adiac ↑	0.4793 0.0187	0.4517 0.0252	0.5586 0.0706	0.6928 0.0116	0.7313 0.0050
Lorenz96 ↓	2.4×10^{-1} 3.6×10^{-2}	2.1×10^{-1} 5.2×10^{-2}	2.6×10^{-1} 2.5×10^{-2}	2.0×10^{-3} 2.0×10^{-4}	1.6×10^{-3} 1.7×10^{-4}
Mackey-Glass ↓	3.4×10^{-2} 3.2×10^{-3}	6.2×10^{-2} 1.5×10^{-2}	5.4×10^{-2} 4.9×10^{-3}	3.0×10^{-2} 1.4×10^{-3}	1.8×10^{-2} 6.5×10^{-3}

ATTRACTORS & AWARENESS

Meta-cognition awareness attractor



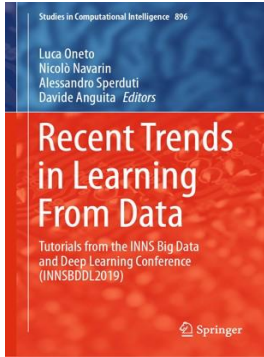
Spatial awareness attractor



Can we map dimensions of awareness into attractor's geometrical properties?

Resources

Deep Randomized Neural Networks



Gallicchio, C. and Scardapane, S., 2020. **Deep Randomized Neural Networks**. In *Recent Trends in Learning From Data* (pp. 43-68). Springer, Cham.

arXiv.org

<https://arxiv.org/pdf/2002.12287.pdf>



AAAI-21 tutorial website:

https://sites.google.com/site/cgallicch/resources/tutorial_DRNN

Reservoir Computing NNs



IJCNN 2021 Tutorial: Reservoir Computing:
Randomized Recurrent Neural Networks



[https://www.youtube.com/
watch?v=XJg7VdN7g-0](https://www.youtube.com/watch?v=XJg7VdN7g-0)



SSIE Summer PhD School of Information
Engineering: Reservoir Recurrent Neural
Networks



[https://www.youtube.com/
watch?v=1K7oJCtTzKQ](https://www.youtube.com/watch?v=1K7oJCtTzKQ)

IEEE Task Force on Reservoir Computing

<https://sites.google.com/view/reservoir-computing-tf/>

Promote and stimulate the development of Reservoir Computing research under both theoretical and application perspectives.



SCAN ME

Summary

- **Reservoir Computing: paradigm for designing and training RNNs**
 - the dynamical reservoir is initialized to be stable (ESP) and left untrained
 - the readout is trained to solve the learning task
- **Fast (& simple) training compared to standard RNNs**
- **The intrinsic state space organization explains the good results on tasks featured by Markovian characterizations**
 - Good for sensor data
- **Very active area of research...**
 - Deep Reservoir Computing
 - Embedded applications
 - Neuromorphic AI
 - Stable RNN architectures
 - Graph Neural Networks

Some arguments for thesis

- **Oscillators-like networks**
- **CNNs for sequential processing (ROCKET-like)**
- **Attractors and Awareness**
- **Modular compositions of RNNs**
- **Structured State Space Models**
- **Improve Edge of Stability RNNs**

Reservoir Computing

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